EE 454 OPTICAL COMMUNICATION SYSTEMS

COURSE CONTENTS

- 1. Introduction to Optical Fibers
- 2. Propagation of Light in Optical Fibers
- 3. Mode Structure in Optical Fibers
- 4. Optical Fiber Communications Link Design
- 5. Attenuation in Optical Fibers, Power Budget Analysis
- **6.** Dispersion in Optical Fiber Communications
- 7. Optical Sources and Detectors used in Optical Fiber Systems
- **8.** Optical Fiber Transmitter
- 9. Optical Receiver Systems
- 10. Introduction to Free Space Optics (FSO) Systems
- 11. Propagation of Light in FSO
- 12. FSO Link Design
- 13. Optical Wireless Communication in Underwater Medium
- 14. All Optical Networking

TEXT BOOK:

1. NAME : Textbook on Optical Fiber Communication and its Applications

AUTHOR : S. C. Gupta

PUBLISHER : PHI Learning Private Limited

ISBN : 978-81-203-4580-5

EDITION : 2012

GRADING:

1 MID TERM EXAM (IN CLASS) : 40 % 1 FINAL EXAM (IN CLASS) : 50 % HOMEWORKS: : 5 % ATTENDANCE: : 5 %

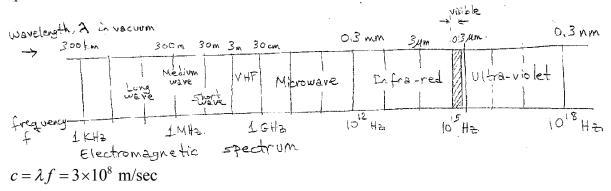
TOTAL: 100 %

Note: It is essential that students show at least 70 % attendance in lectures.

1. Introduction to Optical Fibers

Optical communication is one of the oldest methods of communicating.

The principle of optical communication is to use the light energy to send a message from one point to another. By light energy we mean the infra-red, visible and ultra-violet regions of the electromagnetic spectrum.



The realization of an optical communication system involves a light source, modulator, (transmitting lens), transmission medium, a light detector, receiver, (repeater), transmitter and receiver electronics, processing.

The simplest system is a man turning a flashlamp on and off and another person watching him.



Here the light source is the flash lamp, turning the switch on and off corresponds to modulation, the transmission medium is the atmosphere, the eye is the detector, human brain is the processor. The data rate we provide depens on how fast we can turn the flashlamp on and off.

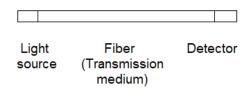
The factors to be considered in such a simple system are:

- The overall cost of the system,
- Frequency of the light source (carrier frequency),
- Frequency should match the operating frequency of the detector,
- Bandwidth of the light source (causes dispersion, i.e., brodening of the received pulse),
- Modulation rate (bir rate with unit bit/second). Limited by the switching electronics. Modulation rate determines the rate of information, i.e., what amount of data can be sent in one second,
- Medium losses (attenuation). Free space loss, absorption and scattering,
- Dispersion in the medium, i.e., widening of the received pulse which results in the reduction of the bit rate that can be used.
- Detector operating frequency that should match the source carrier frequency,
- Detector response time which should be fast enough to accomodate the modulation rate

If the distance is long then a person will be in the middle to convey the message (repeater).

Types of optical communication systems:

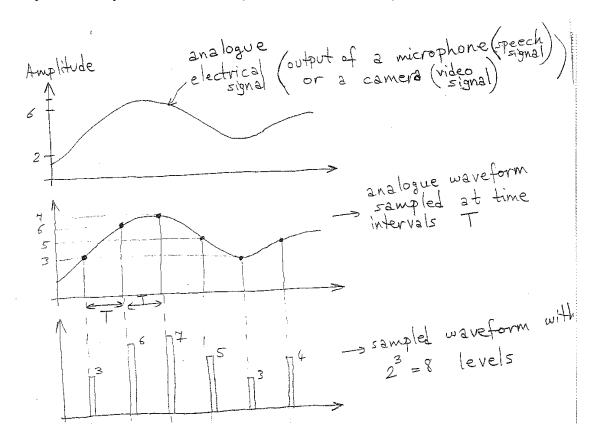
- a) Free space systems. Space-to-space satellite links. (Unguided).
- b) Atmospheric systems. Horizontal terrestrial links, earth to satellite links, satellite to earth links. (FSO, Free Space Optics) (Unguided)
- c) Oceanic (underwater) systems. Guided systems with optical fiber and unguided wireless systems.
- d) Optical fiber systems under and above the ground. Guided.

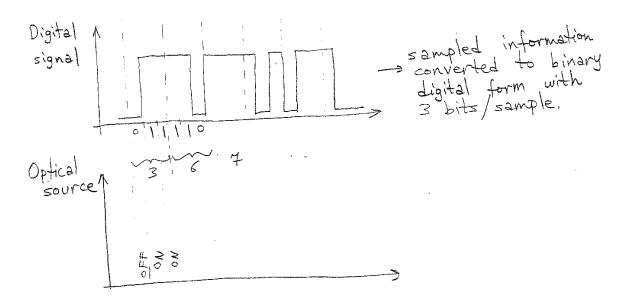


Advantages of optical fiber systems over the coaxial twisted wire systems:

- High repeater spacing possible (100 km or more),
- Potential of extremely high data bit rate. Terabit per second = 10¹² bps or more. Around million million TV channels or billions of telephone channels or Tbps internet traffic,
- Low weight,
- Low cost,
- No electromagnetic interference (EMI),
- High security. Tapping of the signal by unauthorized persons is not possible.

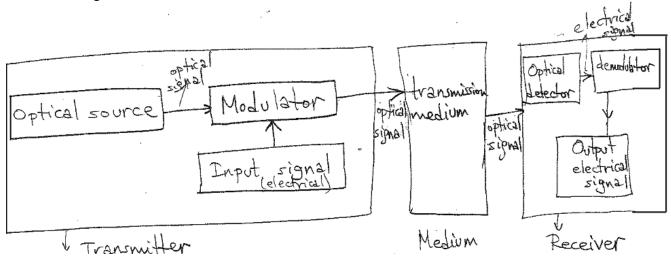
Most optical fiber systems utilize PCM (Pulse Code Modulation).





Basic optical communication system architecture

Block diagram:

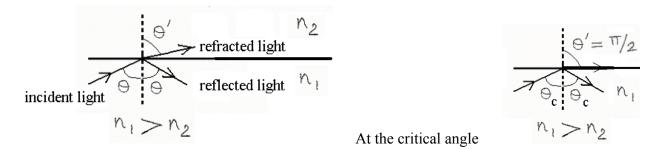


Main components of optical fiber systems:

- 1. The optical source: LED (semiconductor), laser diode (semiconductor),
- 2. A means of modulating the optical output from the source with the signal to be transmitted (internal modulation),
- 3. The transmission medium: Step index fibers (single mode, multimode), graded index fibers (multimode)
- 4. The photodetector which converts the received the received optical power back into an electrical signal. Pin (semiconductor), avalanche (semiconductor),
- 5. Electronic amplification and signal processing required to recover the signal and present it in a form suitable to use.
- 6. Connectors (source to fiber, fiber to fiber, fiber to photo detector) and splicing (fiber to fiber).

2. Propagation of Light in Optical Fibers

Total internal reflection



From Snell's Law, $n_1 \sin \theta = n_2 \sin \theta'$

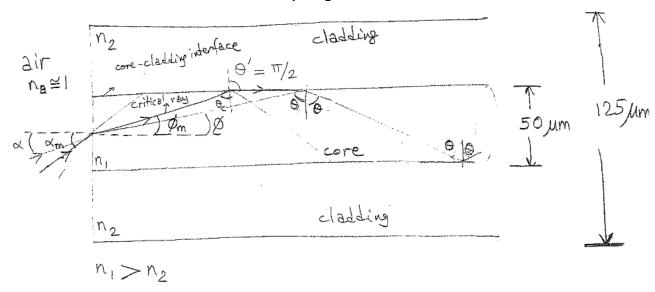
 $\theta_c \triangleq \theta$ at which $\theta' \triangleq \pi/2$ is the critical angle

Thus when
$$\theta' \triangleq \pi/2$$
, $n_1 \sin \theta_c = n_2 \sin(\pi/2) = n_2 \Rightarrow \theta_c = \arcsin(n_2/n_1)$.

For $\theta > \theta_c$, total internal reflection occurs with no losses at the boundary and the light ray is totally reflected at the interface.

i.e., when θ is increased, there appears an angle $\theta = \theta_c$ (called the critical angle) where the refracted ray becomes parallel to the interface. If θ is further increased (i.e., for $\theta > \theta_c$) all the energy contained within the incident light ray is reflected back into the same medium (i.e., the core) so no energy is refracted into the second medium. Thus, no energy is lost. This phenomenon is called total internal reflection.

Considering a cylindrical glass fiber where $n_1 > n_2$:



The ray enters the end face of the fiber from the outside (refractive index of air $=n_a=1$).

For $\theta > \theta_c$, total internal reflections will occur and the ray will propagate along the fiber (in the core) without loosing energy.

Writing Snell's Law at the air to fiber boundary

$$n_a \sin \alpha = n_1 \sin \phi = n_1 \sin \left(\frac{\pi}{2} - \theta\right) = n_1 \cos \theta$$

For
$$n_a = 1$$
, $\sin \alpha = n_1 \cos \theta$,

For the critical ray, $n_a \sin \alpha_m = \sin \alpha_m = n_1 \cos \theta_c$

Inside the core, $n_1 \sin \theta_c = n_2 \sin (\pi/2) \Rightarrow n_1 \sin \theta_c = n_2 \Rightarrow \sin \theta_c = \frac{n_2}{n_1}$

So
$$\cos \theta_{c} = \sqrt{1 - \left(\frac{n_{2}}{n_{1}}\right)^{2}} = \sqrt{\frac{n_{1}^{2} - n_{2}^{2}}{n_{1}^{2}}} = \frac{\left(n_{1}^{2} - n_{2}^{2}\right)^{0.5}}{n_{1}}$$

Thus,
$$\sin \alpha_m = (n_1^2 - n_2^2)^{0.5}$$

Let
$$\Delta n = n_1 - n_2$$
 and $n = \frac{n_1 + n_2}{2}$

$$\sin \alpha_m = (2n\Delta n)^{0.5}$$

 \therefore The greater the value of α_m , the greater is the proportion of the light incident onto the end face that can be collected by the fiber and be propagated by internel reflection.

 $n_a \sin \alpha_m$ is defined as the <u>numerical aperture</u> (NA) which is a measure of light gathering power (acceptance cone) of the optical fiber. For $n_a = 1$, $NA = \sin \alpha_m = (n_1^2 - n_2^2)^{0.5}$.

Conclusion is that in order for the fiber to guide the light, angle of incidence to fiber (α) should be less than α_m .

If $\alpha > \alpha_m$, then refraction will occur at the core-cladding interface and the optical power is lost.

3. Mode Structure in Optical Fibers

Waveguide equations, wave and ray optics

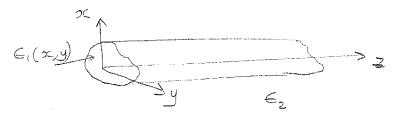
Propagation of light within the fiber can be formulated using either the wave optics or the ray optics.

In wave optics, field theory is used to derive a wave equation in terms of the longitudinal components of the fields in the guide. Then using the transformation equation (derived using Maxwell's equations) the transverse components of the fields are found in terms of the longitudinal components. Various solutions of the wave equation determine the propagation of the modes within the fiber.

In ray optics, propagation of the modes are presented by rays following different paths.

Basic waveguide equations; Wave optics

Consider the waveguide structure



- Assume that the propagation is in z-direction with a longitudinal propagation constant β (i.e., β is the longitudinal component of the propagation vector \overline{k}).
- Assume that the permittivity $\varepsilon(x, y)$ does not depend on z but can vary with x and y. However, it is assumed to vary small amounts over the region of the wavelength so ε is taken as constant.

The fields in a waveguide can be written as

$$\overline{\mathbf{E}} = E_x \hat{\mathbf{a}}_x + E_y \hat{\mathbf{a}}_y + E_z \hat{\mathbf{a}}_z$$

$$\overline{\mathbf{H}} = H_x \hat{\mathbf{a}}_x + H_y \hat{\mathbf{a}}_y + H_z \hat{\mathbf{a}}_z$$
(1)

where for $e^{j\omega t}$ time dependence $E_x = E_{x0}(x,y)e^{-j\beta z}e^{j\omega t}$

$$E_{y} = E_{y0}(x, y)e^{-j\beta z}e^{j\omega t}$$

$$E_{z} = E_{z0}(x, y)e^{-j\beta z}e^{j\omega t}$$
(2)

Here β = propagation constant in z-direction is to be determined.

Using the Maxwell's equations

$$\nabla \times \overline{\mathbf{E}} = -\frac{\partial \overline{\mathbf{B}}}{\partial t} = -\mu \frac{\partial \overline{\mathbf{H}}}{\partial t}$$

$$\nabla \times \overline{\mathbf{H}} = \frac{\partial \overline{\mathbf{D}}}{\partial t} = \varepsilon \frac{\partial \overline{\mathbf{E}}}{\partial t}$$
(3)

$$\left(\frac{\partial E_z}{\partial y} - \frac{\partial E_y}{\partial z}\right) \hat{\mathbf{a}}_x + \left(\frac{\partial E_x}{\partial z} - \frac{\partial E_z}{\partial x}\right) \hat{\mathbf{a}}_y + \left(\frac{\partial E_y}{\partial x} - \frac{\partial E_x}{\partial y}\right) \hat{\mathbf{a}}_z = -\mu \frac{\partial H_x}{\partial t} \hat{\mathbf{a}}_x - \mu \frac{\partial H_y}{\partial t} \hat{\mathbf{a}}_y - \mu \frac{\partial H_z}{\partial t} \hat{\mathbf{a}}_z \tag{4}$$

$$\left(\frac{\partial H_z}{\partial y} - \frac{\partial H_y}{\partial z}\right) \hat{\mathbf{a}}_x + \left(\frac{\partial H_x}{\partial z} - \frac{\partial H_z}{\partial x}\right) \hat{\mathbf{a}}_y + \left(\frac{\partial H_y}{\partial x} - \frac{\partial H_x}{\partial y}\right) \hat{\mathbf{a}}_z = \varepsilon \frac{\partial E_x}{\partial t} \hat{\mathbf{a}}_x + \varepsilon \frac{\partial E_y}{\partial t} \hat{\mathbf{a}}_y + \varepsilon \frac{\partial E_z}{\partial t} \hat{\mathbf{a}}_z$$

From Eq. (2),
$$\frac{\partial E_x}{\partial t} = j\omega E_x$$
 and $\frac{\partial E_x}{\partial z} = -j\beta E_x$ (5)

Substituting Eq. (5) into Eq. (4) and writing in component form

$$\frac{\partial H_z}{\partial v} + j\beta H_y = j\omega \varepsilon E_x \tag{6a}$$

$$-j\beta H_x - \frac{\partial H_z}{\partial x} = j\omega \varepsilon E_y \tag{6b}$$

$$\frac{\partial H_{y}}{\partial x} - \frac{\partial H_{x}}{\partial y} = j\omega \varepsilon E_{z},\tag{6c}$$

$$\frac{\partial E_z}{\partial y} + j\beta E_y = -j\omega\mu H_x,\tag{7a}$$

$$-j\beta E_{x} - \frac{\partial E_{z}}{\partial x} = -j\omega\mu H_{y}, \tag{7b}$$

$$\frac{\partial E_y}{\partial x} - \frac{\partial E_x}{\partial y} = -j\omega\mu H_z \tag{7c}$$

To express E_x, E_y, H_x, H_y in terms of E_z, H_z , we use Eqs. (6a) and (7b) to obtain

$$j\omega\varepsilon E_{x} = \frac{\partial H_{z}}{\partial y} + \frac{j\beta}{-j\omega\mu} \left(-j\beta E_{x} - \frac{\partial E_{z}}{\partial x} \right) \tag{8}$$

Multiplying Eq. (8) by $-j\omega\mu$ and rearranging

$$E_{x} = -\frac{j}{\kappa^{2}} \left(\omega \mu \frac{\partial H_{z}}{\partial y} + \beta \frac{\partial E_{z}}{\partial x} \right)$$
 (9)

where $\kappa^2 = k^2 - \beta^2$ and $k^2 = \omega^2 \mu \varepsilon$

Similarly from Eqs. (6b) and (7b) we obtain

$$E_{y} = -\frac{j}{\kappa^{2}} \left(\beta \frac{\partial E_{z}}{\partial y} - \omega \mu \frac{\partial H_{z}}{\partial x} \right)$$

From
$$\frac{\partial E_z}{\partial y} + j\beta E_y = -j\omega\mu H_x$$
 and $-j\beta H_x - \frac{\partial H_z}{\partial x} = j\omega\varepsilon E_y$, we obtain $H_x = -\frac{j}{\kappa^2} \left(\beta \frac{\partial H_z}{\partial x} - \omega\varepsilon \frac{\partial E_z}{\partial y}\right)$

From
$$-j\beta E_x - \frac{\partial E_z}{\partial x} = -j\omega\mu H_y$$
 and $\frac{\partial H_z}{\partial y} + j\beta H_y = j\omega\varepsilon E_x$, we obtain $H_y = -\frac{j}{\kappa^2} \left(\beta \frac{\partial H_z}{\partial y} + \omega\varepsilon \frac{\partial E_z}{\partial x}\right)$

$$E_{y} = -\frac{J}{K^{2}} \left(\frac{\partial E_{z}}{\partial y} - \omega \mu \frac{\partial H_{z}}{\partial x} \right)$$
From $(7a)$ and $(6b)$

$$H_{x} = -\frac{J}{K^{2}} \left(\frac{\partial H_{z}}{\partial x} - \omega \epsilon \frac{\partial E_{z}}{\partial y} \right)$$

$$Hy = -\frac{J}{K^2} \left(\frac{3Hz}{3y} + w \in \frac{3E_z}{3x} \right)$$
 (2)

Now let us solve for Ez and Hz so that from @-12 we can get the transverse fields.

Subst. (1) and (12) into (6c) and mult. by $\frac{j k^2}{w \in w}$

$$\nabla_{T}^{2} E_{2} + K^{2} E_{2} = 0$$
where
$$\nabla^{2} - \partial^{2} = \partial^{2} + \sum_{k=1}^{2} (13)^{k} = 0$$

where
$$\nabla_{1}^{2} = \frac{\partial^{2}}{\partial x^{2}} + \frac{\partial^{2}}{\partial y^{2}} = \text{transverse laplacian operator.}$$

Similarly

$$\nabla_{T}^{2}H_{2} + K^{2}H_{Z} = 0$$

Modes	Longitudinal components	Transecte
TEM (tranverse electromagnetic	Ez=0 Hz=0	ET , HT
TE (tranve electric)	H2 #0	€ +, H,
TM(transver	HZ=0 Ez+0	//
HE or EH (hybrid)	Ez = 0 Hz = 0	//

In cylindrical coordinates one can obtain by transforming

$$E_{\phi} = -\frac{J}{K^{2}} \left(\beta \frac{1}{r} \frac{\partial E_{z}}{\partial \phi} - \omega_{x} \frac{\partial H_{z}}{\partial r} \right)$$

$$H_{r} = -\frac{J}{K^{2}} \left(\beta \frac{\partial H_{z}}{\partial r} - \omega_{e} \frac{1}{r} \frac{\partial E_{z}}{\partial \phi} \right)$$

$$H_{\phi} = -\frac{J}{K^{2}} \left(\beta \frac{1}{r} \frac{\partial H_{z}}{\partial \phi} + \omega_{e} \frac{\partial E_{z}}{\partial r} \right)$$

Ray Optics and Ray Equations

Ray optics describes the propagation of light in the form of rays. Ray optics can be applied to all phenomena that are described by the wave equation and that satisfy the requirement that is short compared to the dimensions of the guide.

Starting with the Helmholtz equation

 $\nabla^2 \vec{E} + k^2 \vec{E} = 0$

If I is any rectangular component of E

$$\nabla^2 \Psi + k^2 \Psi = 0 \qquad -$$

where $k = nk_0 = n\left(\frac{2\pi}{\lambda_0}\right)$ propagation constant is vacuum

A solution in the form $\Psi = \Psi_0(x,y,z) e^{-jk_0 S(x,y,z)}$

will be looked for. Here Yo and 5 are real functions of position. S(x,y,z) being the phase function associated with the medium and is called an "eikonal".

Substituting (2) into (1) and performing some algebra, it can be shown that for $\lambda_0 \to 0$

 $\nabla S = N$

known as the eikonal equation which determines the function S that defines the surfaces of constant phase by the equation

$$5(x, y/z) = constant.$$

The light rays are defined as the locus of points that form the orthogonal trajectomies to the constant phase fronts of a light wave. i.e. if constant phase surfaces are known, one can construct the light rays by drawing lines perpendicular to the phase fronts. However it is often desirable to find the ray trajectories directly without having to construct the phase fronts.

—> Without derivation we state the paraxial (rays are nearly parallel to the z-axis) ray equations in cylindrical coordinates (r, \emptyset, z) as:

$$\frac{d^2r}{dz^2} - r\left(\frac{d\phi}{dz}\right)^2 = \frac{1}{n_0} \frac{\partial r}{\partial r}$$

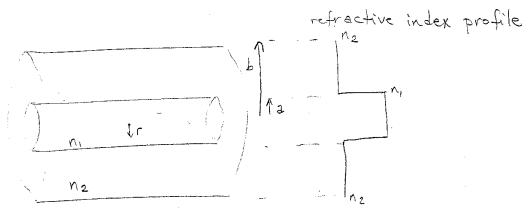
$$\frac{d}{dz} \left(r^2 \frac{d\phi}{dz}\right) = \frac{1}{n_0} \frac{\partial r}{\partial \phi}$$

$$\Rightarrow \text{In ray optics}$$

note mode mode mode was path of lowest order mode

The Step Index Fiber

The step index fiber has homogeneous core and homogeneous cladding.



Assumption: b is large enough so that the cladding field decays exponentially and approaches zero at the cladding-air interface.

Equations satisfying Ez and Hz in cylindrical coord.

are! 12 p2

$$\frac{\partial^{2} E_{z}}{\partial r^{2}} + \frac{1}{r} \frac{\partial E_{z}}{\partial r} + \frac{1}{r^{2}} \frac{\partial^{2} E_{z}}{\partial \phi^{2}} + K^{2} E_{z} = 0$$

Longitudinal direction of propagation is in z-direction time dependence is just so that fields have dependence of the form ej(wt-PZ)

Using separation of variables in 1

Since fiber has circular symmetry, we choose

$$\widehat{\mathbb{D}}(\widehat{\phi}) = e^{\widehat{\mathbf{J}} \sqrt{\widehat{\phi}}}$$

where I is (thre or The indeger and

$$E_z = A F(r) e^{j \gamma \beta}$$

Using 4 in 1) and mult. by /Aejrø we have

$$\frac{d^{2}F(r)}{dr^{2}} + \frac{1}{r}\frac{dF(r)}{dr} + \left(K^{2} - \frac{v^{2}}{r^{2}}\right)F(r) = 0$$

This is a form of Bessel's equation. The solution should have the following properties:

(i) The field in the core must be finite at r=0

(ii) Cladding field must have an exponentially decaying behavior at large distances from the center of the fiber.

The proper solution for @ is

$$E_{z} = \begin{cases} A J_{\nu}(Kr) e^{j\nu \phi}, & r < a \\ C H_{\nu}(j r) e^{j\nu \phi}, & r > a \end{cases}$$

Similarly
$$H_{2} = \begin{cases} B J_{\nu}(kr) e^{j\nu\phi}, r < a \\ D H_{\nu}^{(0)}(j r) e^{j\nu\phi}, r > a \end{cases}$$

where JV is the Bessel function of order V

H(1) " " modified Hankel function of the

first kind of order V

A,B,C,D are unknown constants.

From Maxwell's equation E_r , E_{δ} , H_r , H_{δ} in the core are found as (i.e transverse fields for r < a) $E_r = -\frac{\dot{J}}{K^2} \left[ABKJ_{\nu}'(Kr) + B(Jv)(WM) + J_{\nu}(Kr) \right] e^{\dot{J}V\delta}$

$$E_{\phi} = -\frac{j}{K^{2}} \left[j_{\beta} \stackrel{\vee}{r} A J_{\nu}(Kr) - Kw_{\mu}B J_{\nu}'(Kr) \right] e^{j\nu\phi}$$

$$H_{r} = -\frac{j}{K^{2}} \left[-j\omega \in \stackrel{\vee}{r} A J_{\nu}(Kr) + KB B J_{\nu}'(Kr) \right] e^{j\nu\phi}$$

$$H_{\phi} = -\frac{j}{K^{2}} \left[K\omega \in A J_{\nu}'(Kr) + j_{\beta} \stackrel{\vee}{r} B J_{\nu}(Kr) \right] e^{j\nu\phi}$$

$$H_{\phi} = -\frac{j}{K^{2}} \left[K\omega \in A J_{\nu}'(Kr) + j_{\beta} \stackrel{\vee}{r} B J_{\nu}(Kr) \right] e^{j\nu\phi}$$

where $K^2 = K_1^2 - \beta^2 = \omega^2 M_0 \in [-\beta^2]$

Similarly the transverse field in the cladding are found as (i.e for r>a).

 $E_{r} = -\frac{1}{8^{2}} \left[P8C H_{\nu}^{(1)} '(j8r) + \omega \mu_{0} \frac{1}{r} D H_{\nu}^{(1)} (j8r) \right] e^{j\nu \phi}$ $E_{\phi} = -\frac{1}{8^{2}} \left[P \frac{V}{r} C H_{\nu}^{(1)} (j8r) - 8\omega \mu_{0} D H_{\nu}^{(1)} '(j8r) \right] e^{j\nu \phi}$ $H_{r} = -\frac{1}{8^{2}} \left[-\omega \epsilon_{2} \frac{V}{r} C H_{\nu}^{(1)} (j8r) + 8PD H_{\nu}^{(1)} '(j8r) \right] e^{j\nu \phi}$

 $H_{\phi} = -\frac{1}{8^{2}} \left[8 \omega \in_{2} \subset H_{V}^{(1)} ' (j8r) + \beta \frac{V}{r} D H_{V}^{(1)} (j8r) \right] e^{jV\phi}$

where $\frac{\partial H_{(j)}^{\lambda}(j r)}{\partial (j r)} = H_{(j)}^{\lambda}(j r)$

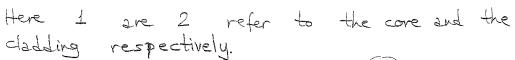
$$y^2 = \beta^2 - k_2^2 = \beta^2 - \omega^2 M_0 \in 2$$

 \rightarrow A, B, C, D and B is to be determined by applying the boundary conditions at the corecladding interface (r=2)

-> Boundary conditions at r=a yield

tangential
$$E_{z_1} = E_{z_2}$$
 at $r = 3$
 $E_z = E_{z_2}$ at $r = 3$
equal $E_{\phi_1} = E_{\phi_2}$...

tangential
$$H_{21} = H_{22}$$
 at $r = a$
H's are \Rightarrow $H_{\phi_1} = H_{\phi_2}$ "

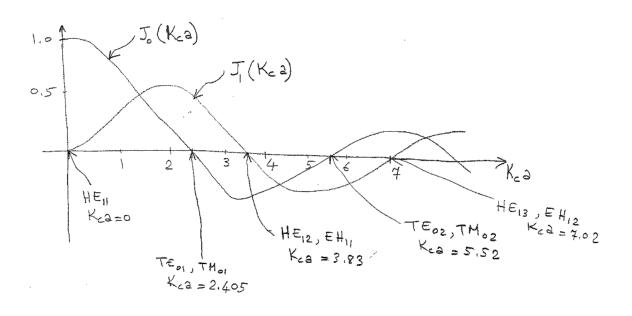


Using @ . (7), (8) and (9) in (10) one can obtain

where
$$W = \begin{bmatrix} J_{V}(Ka) & 0 & -H_{V}(Jra) & 0 \\ \frac{J}{a} \frac{F}{K^{2}} J_{V}(Ka) & \frac{J}{K} \frac{W_{U}}{J_{V}}(Ka) & \frac{J}{a} \frac{F}{K^{2}} H_{V}^{(j)}(Jra) & -\frac{J}{V} \frac{W_{U}}{J_{V}}(Jra) & \frac{J}{a} \frac{F}{K^{2}} J_{V}(Ka) & \frac{J}{a} \frac{F}{K^{2}} J_{V}(Ka) & \frac{W_{U}}{K} \frac{J}{V_{U}}(Jra) & \frac{J}{a} \frac{J}{V^{2}} H_{V}^{(j)}(Jra) & \frac{J}{a} \frac{J}{V^{2}} H_{V}^{(j)}(Jra) & \frac{J}{a} \frac{J}{V^{2}} H_{V}^{(j)}(Jra) & \frac{J}{a} \frac{J}{V^{2}} H_{V}^{(j)}(Jra) & \frac{J}{a} \frac{J}{V^{2}} \frac{J}{V_{U}}(Jra) & \frac{J}{a} \frac{J}{V^{2}} \frac{J}{V_{U}}(Jra) & \frac{J}{a} \frac{J}{V^{2}} \frac{J}{V_{U}}(Ka) & \frac{J}{a} \frac{J}{V_{U}}(Jra) & \frac{J}{A} \frac{J}{$$

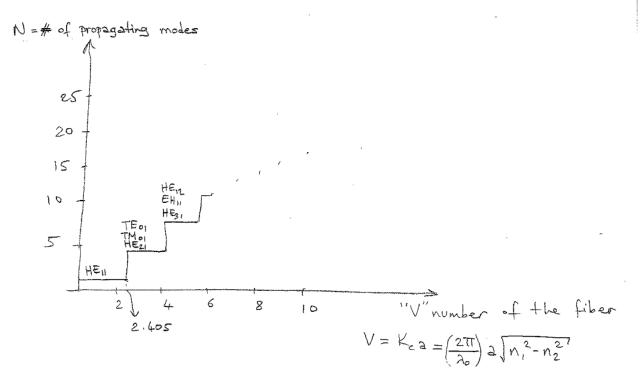
Mode cutoff conditions

i or $X = 0 = \sqrt{\frac{2}{B_1^2 - k_{20}^2}}$ and detaches from the guide k2c = W2 Mo € > permittivity of the cladding. In the core at cut off K2 = k1c - B2 = W2 MOE, - B2 =, W2 MOE, - W2 MOE, - W2 MOE $\Rightarrow \qquad \mathcal{W}_{c} = \frac{K_{c}}{\sqrt{M_{o}(\epsilon_{1} - \epsilon_{2})}}$ cutoff frequency of a mode -> Cutoff frequency of a mode can be zero if K=0 → Only HE mode can exist in an optical filen with we=0 i.e it is possible to design a single mode fiber. -> Working on the characteristic equ. (12), letting x → 0 and using the approximation for the modified Hankel function for small arguments the cutoff conditions are obtained -> TE and TM modes 1=0 Cutoff conditions for TEOM and TMOM modes are obtained from the ut root of J (Ka)=1 -> HEIM modes Cut off condition Ke2 = xvu for M=1,2,3 where x /m is the Mth root of Jy (xx/M)=c HE mode exists for all frequencies. 1 -> EHVM modes Cut off condition same as except OCYM + 0



$$\rightarrow$$
 HEym modes for $V=2,3,4,...$

$$\left(\frac{E_1}{E_2}+1\right)J_{V-1}\left(K_ca\right)=\frac{a\ Kc}{V-1}J_{V}\left(K_ca\right)$$
determines the cutoff condition



= $\frac{2\pi}{20}$ a (NA) if N is large = $\frac{2\pi}{20}$ a (NA) if N is large = $\frac{4V^2}{\pi^2}$ or $\frac{V^2}{2}$ Total no. of modes (N) in a step index fiber = $\frac{4V^2}{\pi^2}$ or $\frac{V^2}{2}$

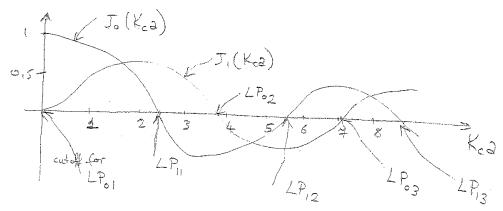
Linearly polarized (LP) modes

Assuming $\Delta = \frac{n_1^2 - n_2^2}{2n_1^2} \ll 1 \implies \Delta \approx \frac{n_1 - n_2}{n_1}$ (weakly solution is simplified $\frac{n_1^2 - n_2^2}{n_1^2} \ll 1$

- Fields are essentially polarized in one direction.

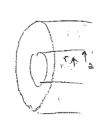
 Ex, Hy, Ez, Hz.
- -> LPam modes are actually a superposition of HEV+1, M and EHV-1, M modes. Here & refers to a superposition of exact modes with labels V+1 and V-1. LP modes are not true modes.
- -> Cutoff condition for LP modes $J_{\ell-1}(K_{c}a) = 0$ For $\ell=0$ \Rightarrow $J_{\ell}(K_{c}a) = 0$

LPOI corresponds to HEII



of HEV+1, 11 and EHV-1, 11 modes and since each has coslop or sin of dependence, each LPIm mode has four discrete HE and EH mode patterns

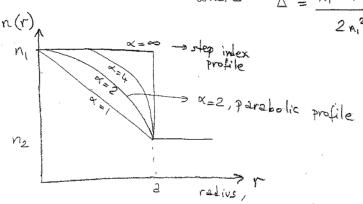
Graded Index Fiber



Refractive index profile

$$n(r) = \begin{cases} n_1 \left[1 - 2\Delta \left(\frac{r}{a}\right)^{\alpha}\right]^{1/2}, r < a \\ n_1 \left(1 - 2\Delta\right)^{1/2}, r > a \end{cases}$$

where $\Delta = \frac{n_1^2 - n_2^2}{2n_1^2}$



-> Bandwilth of graded index fiber ~ 300 MHz-km -

whereas for step index, bandwidth of the fiber < 100 MHz-km.

Ray optics analysis of the graded-index fiber

Ray trajectory will be found by solving the ray equation. Without derivation we write the paraxi vay equations as

$$\frac{d}{dz}\left(r^2\frac{d\phi}{dz}\right) = \frac{1}{n_1}\frac{\partial n}{\partial \phi}$$

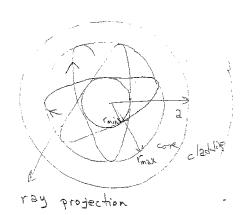
$$\frac{d^2r}{dz^2} - r\left(\frac{d\phi}{dz}\right)^2 = \frac{1}{n_1} \frac{\partial n}{\partial r}$$

The refractive index does not change wir to \$. Thus an = 0. Using this in 3 and integrating

$$r^2 \frac{dq}{dz} = c_1 \implies \frac{dz}{dz} = \frac{r^2}{c_1}$$

For A << 1 $\kappa(r) = \kappa_1 \left[1 - \left(\frac{r}{2} \right)^2 \Delta \right]$ $\frac{\partial n}{\partial r} = -2n_1 \left(\frac{\Delta}{3^2}\right) r$ · Substi @ and 5 into 4 $\frac{d^{2}r}{dz^{2}} + 2 \frac{\Delta}{dz^{2}} r - \frac{c_{1}^{2}}{r^{3}} = 0$ Eq. (8) will yield r(2) as (without showing the intermedial steps) $r(z) = A \left\{ 1 + \sqrt{1 - b^2} \sin \left[2 \sqrt{2} \left(z - z_0 \right) \right] \right\}^{1/2}$ Using (3) in (5) and integrating we find $\phi(z) = \phi_0 + \arctan \left\{ \sqrt{1-b^2} + \tan \left[\Omega(z-z_0) \right] \right\}$ gronstant where $A = \sqrt{c_3}$ constant $\Omega = \sqrt{2\Lambda}$ $b^2 = C_1^2 \left(\frac{S_2}{R_3} \right)^2$ scheck -> r(z) and \$\phi(z)\$ describe the ray trajectory. -> From (3) it is observed that the ray is trapped inside the fiber core between two turning points rmax and rmin given by $r_{\text{max}} = A \left(1 + \sqrt{1 - b^2} \right)^{1/2}$ $v_{min} = A \left(1 - \sqrt{1 - b^2}\right)^{1/2}$

-> The rays spiral down the fiber between rmax and rmin



Special cases for 0, 0The predictional rays ϕ does not change winto . \Rightarrow reduces to $\Rightarrow b=0$, it can be shown that 0 $r(z) = \sqrt{2} A \sin \left[\mathcal{L}(z-z_0) + \frac{\pi}{4} \right]$ Also for b=0, 0 reduces to $\phi(z) = \phi_0 + \frac{\pi}{2}$, i.e. ϕ is a constant.

(13) and (14) shows that the ray moves on a sinusoidal trajectory in the meridional plane crossing the axis r=0 (meridional ray) as it propagates down the z-axis. Spatial radian frequence of this sinusoidal meridional ray is so.

-> The other special case occurs when b=1

$$r(z) = A$$
 (5)
 $\phi(z) = \phi_0 + (z - z_0) \Sigma$ (6)

This ray described by ID and IB is known as the helical ray since the ray travels at a fixed distance from the axis (r=A) on a helical path described by IB.

Meridional and helical rays are the limiting cases. The general ray will travel along a spiraling trajectory whose distance from the liber axis varies periodically between the turning

-> Total no. of modes in a graded index fiber is found for the refractive index profile given by D as

$$N = \frac{V^2}{2} \left(\frac{\alpha}{\alpha + 2} \right) -$$

where V = V'' number = $k_0 = \sqrt{n^2 - n^2} \approx k_0 = n_1 \sqrt{2} \sqrt{n_1^2 - n_2^2}$ and for step index fiber $\alpha = \infty \implies N_{\text{step}} = \frac{V^2}{2}$ for parabolic index fiber $\alpha = 2 \implies N_{\text{parabolic}} = \frac{V^2}{4}$ i've $N_{\text{parabolic}} = \frac{N_{\text{step}}}{2}$

i.e. total no. of modes in a graded index waveguide with a parabolic profile $(\kappa=2)$ is half the no. of modes that exist in a step index fiber.

4. Optical Fiber Communications Link Design

will discuss point-to-point link Procedure
-> Examine the components available for the particular application. The components to choose are:
1. LED or laser diode optical source - emission wavelength - spectral line width - optical output power - effective radiating area - emission pattern - medulation rate 2. Multimode (step or graded index) or single-mode optical fiber
- Core radius - Core refractive-index profile - Bandwidth (Dispersion limitation) - Attenuation - Numerical Aperture 5. Pin or avalanche photodiode - Responsivity - Operating wavelength - Speed (response time) - Sensitivity (NEP)
-> See how these components relate to the system performance criteria. System performance requirements are 1. The desired (or possible) transmission distance 2. The data rate or channel bandwidth 3. Bit error rate (BER) -> For the given set of components and system performance — Carry out a power hidget analysis to

determine whether the link meets the attenuation requirements or if repeaters are needed. Carry out a system rise time analysis to verify that the overall system performance requirements are met. _ If performance requirements are not met, change appropriate components and repeat the same procedure. 'Try 'several designs to find the cheapest design. Design Considerations -> Choose the operating wavelength -If path length is not long choose 0.8-0.9 um range — If " " long choose 1.55 mm for low data rates
— " " " " " " " 1.3 mm " high " " -> Choose the characteristics of two of the main building blocks (transmitter, fiber-receiver) and calculate the characteristics of the remaining third one, Check whether the system requirements are met Choosing Photodetector - Determine the minimum optical power received by the photodetector to satisfy the required bit error rate (BER) Keep in mind that simpler (cheaper)
pin photodiode receiver is smore stable with temperature changes - Keep in mind that : I smaller bias voltager avalanche photodiodes have - higher sensitivity

a valanche photodiodes have - higher sensitivity

(ie can detect lower optical power thus increasing the repeater spacing)

Choesing the light source

- Parameters to be taken into consideration are: Data rate, transmission distance, cost, dispersion.

	Keep in mind that
.*	LED is cheaper no feedback orth is needed for temperature stabilization has lower life time
	laser > has narrower spectral width > has higher coupling efficiency (can couple 10-15 dB more power than LED) has higher modulation rate
	LED at 1.3 μ m = 150 (Mb/s) km.
	laser at $0.8-0.9$ $2.5(Gb/s) km$ [aser " 1.3 mm $3 > 25(Gb/s) km$.
	Odial Tilan
	Choosing the Uprical riber - Depends on the type of the light source employed and on the maximum amount of dispersion that can be tolerated.
	_ Check the attenuation characteristics of the fiber
	and the cabling. — Check the splice, connector and other losses.
	- Keep in mind that
	single made fiber -> can be used with laser > yields the maximum bit rate-distance
	has more difficult splicing.
	ten index multimode fiber -> can be used with LED and law
	-> cheaper
	> good for low bit referditence products.
	graded index fiber -> can handle higher bit-rate-distant
	products as compared to step-intex multimode filer, yet much
	easier splicing as compared to single mode fiber.

Link Power Budget

 \rightarrow Loss in an element = 10 log $\frac{P_{\text{out}}}{P_{\text{in}}}$ (LB)

where Pout = output optical power of that specific element
Pin = input " "

light source of the splice source of the sou

PT = Ps - PR

total optical optical power sensitivity

power loss at the end of

the fiber flylead
attached to source

Rise Time Budget

-> Performed to determine the dispersion limitation of the fiber link.

tsys = (tx + tmat + tmod + troc)

total rise time the is tmat is tmod is

of the link the rise the material the modal receiver

time of the dispersion dispersion rise time of the fiber

of the fiber

the results from the rise time of the source and its drive circuitry.

-> to can be estimated from Eq. 4-28 of Keiser's book (can be found from Fig 3-13 of =0.5 for steady state modal equilibrium =1 for little mode mixing =0.7 practical value Here BM= Bo -> tmod = 440 L2 (in km) in usec ? I'm (MHZ) -> trac results from the photodetector rise time and the 3-dB electric bandwidth of the receiver front end. (Broc) $\frac{1}{\text{winsec}} = \frac{350}{\text{Brz}} = \frac{350}{\text{(in MHz)}}$ empirical formula tsys should be less than \$ 70 % of an NRZ (non-return to zero) bit period

35% of an RZ (return-to-zero) bit period | tsys \ \frac{0.7}{data rate} \Rightarrow design is O.K | The lift has been design | the lift has bee for RZ, replace 0.7 by 0.35 Check the cost of the overall system and try other designs to find a cheaper one

An example

Perform the power budget and the rise time budget of an optical fiber link with 20 Mb/s data rate (NRZ) formal) and 10-9 bit error rate. Determine the maximum repeaterless transmission distance for the denon.

-> Pick a silicon pin photodiode at 0.85 mm. From Fig. 8-3 of Keiser

 $\begin{array}{ccccc} P_R & -201 & & & \\ P_R & -30 & & & \\ (receiver & & \\ Sensitivity) & -40 & & \\ \hline (dB_m) & & & \\ \end{array}$ $\begin{array}{ccccccc} F_R G_2 A_5 & Pin & & \\ \hline (h3, \mu m) & & \\ \hline \end{array}$ $\begin{array}{ccccc} F_R G_2 A_5 & Pin & & \\ \hline \end{array}$ $\begin{array}{ccccc} F_R G_2 A_5 & Pin & & \\ \hline \end{array}$

-50 -60 SI APD (0.8-0.9 µm) -70 (0.8-0.9 µm)

For Si pin photodiode at 0.85 mm, PR = -42 dBm for 20 Mb/data rate

— Pick a GaAl As LED that can couple $50\mu\text{W}(-134B_m)$ average optical power into a fiber flylead with soum core diameter i.e. $\mathbf{r}_{\!\!\!S}=-13\,dB_m$

 $P_T = P_S - P_r = -13 dB_m - (-42dB_m) = 29dB_m$

-> Assume 1 dB loss at the fiber flylead to cable connector and a 6 dB system margin.

: 29 dB = 2 (1 dB) + x L + 6 dB

«fL = 21 JB

-> If $\alpha_f = 3.5 \, dB/km$ for the fiber you pick, then $L = \frac{21}{3.5} = 6 \, km \implies \text{This is the repeaterless transmission}$ distance

For graphical representation see Fig. 8-4 of Keiser's book,

For the rise time budget analysis

→ Assume LED and its drive circuitry has t_{toc} = 15 ns → From Fig. 3-13 of Keiser / D_{mat} = 87.5 ps/nm. km at λ=0.85μm Typical spectral width Gof LED = 40 nm

in transmission that = Dmat of L = 87.5 Ps/nm.km x 40 nm x 6 km

tmot = 21 nsec.

-> If the fiber selected has 400 MHz. Em bandwidth distance product the if B = 400 MHz

and q=0.7 for practical values

$$t_{\text{mod}} = \frac{440 \text{ L}_{\pm}^{4}}{\text{Bo}} \text{ in } t_{\text{m}} = \frac{440 \times 6^{(0,7)}}{400} \approx 3.9 \text{ nsec.}$$

- For further information on mode coupling effect ise the choice of q read sec. 3-5 of Keiser. Actually for the first 0.1-0.55 km of fiber length q = 1, BxL " I fiber leights >> 0.55 km q=0.5=mode making Reasonable estimate for q is 0.7 By xVII
- Assuming the 3dB electric bandwidth of the receiver is $25 \text{ MHz} = \frac{1}{277R_{+}C_{T}}$

$$t_{rx} = \frac{350}{25} = 14 \text{ ns}$$

:
$$t_{sys} = [(15 \text{ ns})^2 + (21 \text{ ns})^2 + (3.9 \text{ ns})^2 + (14 \text{ ns})^2]^{1/2}$$

$$\approx 29.6 \text{ ns}$$

$$\frac{0.7}{\text{data rate}} = \frac{0.7}{20 \,\text{Mb/s}} = 35 \,\text{ns}$$

tsys = 29,6 ns < 35 ns

: the design is O.K based on rise time budget -> Check the cost of the overall system and try other derigns

5. Attenuation in Optical Fibers, Power Budget Analysis

- 1. Attenuation, he power loss in fibers
 - Absorption losses
 - Scattering losses
 - Radiative losses (Bending, microbending, waveguide losses)
 - 2. Dispersion, he broadening of a pulse at the receiving end of the fiber
 - Intramodal dispersion.
 - Material Lispersion
 - Waveguide dispersion
 - Intermodal dispersion

Attenuation

- --- Determines the maximum distance between a transmitter and a receiver
- \rightarrow Signal attenuation is defined as $\alpha = [10 \log(Pin/Pout)]/L db/km$.

No loss => Pout = Pin >> x = 0 1B/km.

-> Actual fiber has in the order of several db/km loss. 0,2 LB/km or even less reported to be feasible.

Absorption

Light is absorbed within the fiber by 3 different mechanisms:

- 1. By atomic defects in the glass composition

 Atomic defects are imperfections of the atomic structure of the fiber such as missing molecules, high-density clusters of atom groups or oxygen defects in the glass structure.
- Attenuation due to atomic effects is not significant in general.

However, it could be important if the fiber is exposed to intense nuclear radiation levels.

2. Extrinsic absorption by impurity atoms in the glass material.

This is the dominant absorption factor in fibers: (prepared by direct melt method)

- Impurity absorption results from ions such as iron, chromium, cobalt, copper and OH (water) ions. Occur from electronic transitions between energy levels associated with the incompletely filled inner subshell of there ions or a method impurities present in the fiber is ~1 or 10 parts in 109 (changes depending on the fiber fabrication method). (auses 1 to 10 dB/km loss
 - -> OH (hyroxyl) ion impurities in fiber preforms results from the oxyhydrogen flame used for the hydrolysis reaction of the SiCl4, Ge Cl4 and POCl3 starting materials.
 - 10° parts for attenuation to be less than 201B/k Large absorption peaks at 1400,950 and 705 n Between these peaks there are regions of low attenuation.
 - 3. Intrinsic absorption by the basic constituent atoms of the fiber material.
 - --> Results from electronic absorption bands in the ultraviolet region and from atomic vibration bands in the near-infrared region.

Scattering

Results from microscopic variations in the material density, from compositional fluctuations or from structural inhomogeneities or defect occurring during manufacturing of the fiber.

-> Glass, being composed of randomly connected molecules, contains regions in which the molecular

density is either higher or lower than the average density in glass.

-> Also glass has several oxides as 5:02, GeO2, P205 so compositional fluctuations can occur.

As a result of these two effects in varies within glass over distances that are small compared to wavelength.

-> Result is Rayleigh scattering (as in molecular scattering in the atmosphere)

Rayleigh scattering has χ^{-4} , i.e ft dependence.

It increases dramatically as frequency increases,
for $\chi < 1 \mu m$, Rayleigh scat, is the dominant loss in fibers. At $\chi > 1 \mu m$, infrared absorption effects tend to dominate optical signal attenuation.

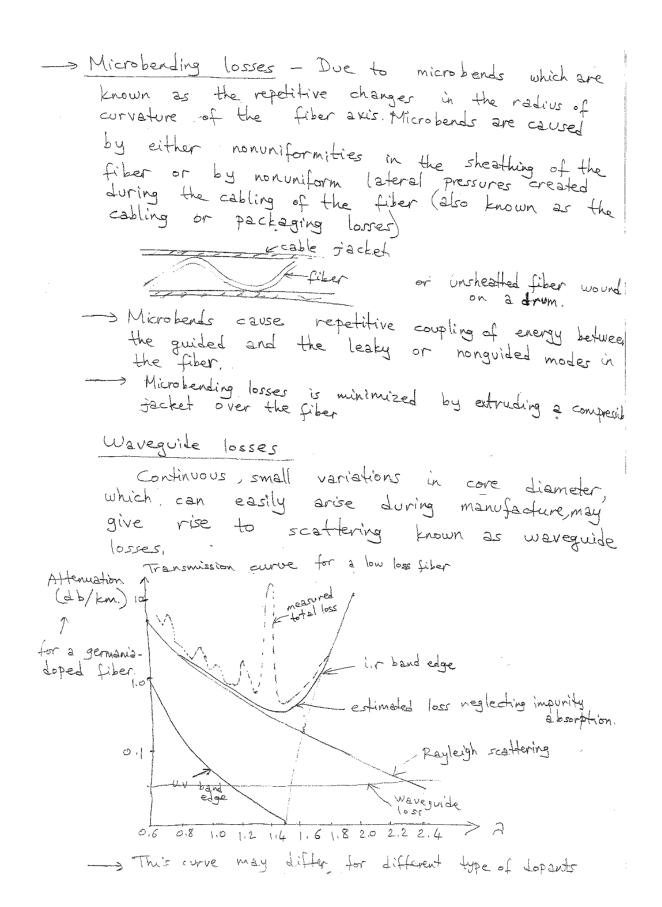
Radiative losses

Bending losses
Losses due to bends in fiber having radii that are large compared to the fiber diameter e.g. when fiber cable turns a corner. As the radius of curvature decreases, loss \nearrow exponentially. It is negligible up to a critical $R = R_c \cong \frac{a}{N_1^2 - n_2^2}$



If R > Rc, loss is considerable (same of the light is not totally internally reflected but propagation to the cladding and is radiated away)

Fiven for R > Rc, the limiting factor is the mechanical properties of the fiber ie a mechanically acceptable (no significant stress cracking) bending radius gives rise to negligible bending loss.



Transmisssion windows (lowest attenuation at $\lambda = 1.55 \ \mu m$ for Germania-doped silica, 1.3 μm has low attenuation, too.

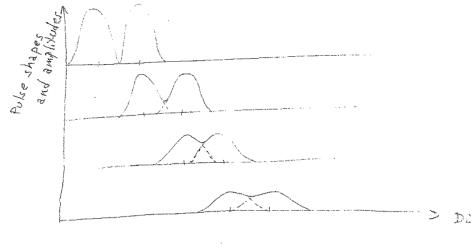
6. Dispersion in Optical Fiber Communications

Dispersion in Optical Fibers

Dispersion is the phenomenon that each frequency component will travel with different velocity due to the fact that the refractive index of the medium is a function of the wavelength.

Dispersion results in the broadening of the light pulse. This pulse broadening causes a pulse to overlap with the neighboring pulses. After a certain amount of overlap has occurred, adjacent pulses can no longer be individually distinguished at the receiver and errors will occur. Thus dispersion properties determine the limit of the information capacity of the fiber.

In step index (multimode) ~ 20 MHz. km.
In graded index (at specific wavelength) ~ 2.5 GHz. km.
In single-mode fiber ~ > 2.5 GHz.km.



> Distance along

-> As a background let us study group velocity

For monochromatic wave having only y-comp, and

propagating in z-direction in a dielectric medium

Ey = A cos (Wt-kz) Setting phase = orn-lant = Wt-kz = const $\omega = \frac{dz}{dt} = \frac{\omega}{k}$ > known as the phase velocity If the wave has two frequencies, w+AW => k+At

 $E_y = E_y' + E_y'^2 = A \left\{ \omega \left[(\omega + \Delta \omega) t - (k + \Delta k) z \right] + \omega \left[(\omega - \Delta \omega) t \right] \right\}$ - (K-DK)=73

Ey = 2A cos (wt-kz) cos (DWt-Dkz) - like AM wave

slowly varying envelope of the carrier

is a group velocity is obtained by setting

DWI-AKZ = const.

and $w_g = \frac{dz}{dt} = \frac{\Delta w}{\Delta k}$ In the limit $\Delta w \to 0$

 $v_g = \frac{dw}{dt} = c \left(\frac{dR}{dt}\right)^{-1}$

-> is actually the phase velocity of the wave envelope and the velocity that information modulate on a wave will propagate at.

-> Examine the casethal a signal modulates an optical source

-> Assume that the modulated optical signal excites all modes equally at the input of the fiber. Lie each mode carries an equal amount of energy through the fiber

-> Each mode contains all of the spectral components in the wavelength band over

which the source emits.

-> The signal may be considered as modulating each of these spectral components in the same way As the signal propagater along the fiber, each spectral component can be assumed to travel independently and to undergo a time delay or group delay in the direction of propagation

 $t_g = \frac{L}{\sqrt{3}} = \frac{L}{c} \frac{dB}{dk} = -\frac{\lambda^2 L dB}{2\pi c}$ (1)

Pulse spread (total delay difference over a distance L) $G_{g} = \frac{d t_{g}}{d \lambda} T_{\lambda}$ (2)

where of -> r.ms spectral width DA

dta -> delay difference per unit wavelength.

Material dispersion

 \rightarrow Due to n being 2 function of $\lambda \Rightarrow \beta = 2T n(\lambda)$

-> Important for single mode waveguide

broader spectrum than Laser diode

group delay resulting from material dispersion

$$t_{\text{mat.}} = \frac{-\lambda^2 L}{2 \text{Tic}} \left[n \left(-\frac{2 \text{Ti}}{\lambda^2} \right) + \frac{2 \text{Ti}}{\lambda} \frac{dn}{d\lambda} \right]$$

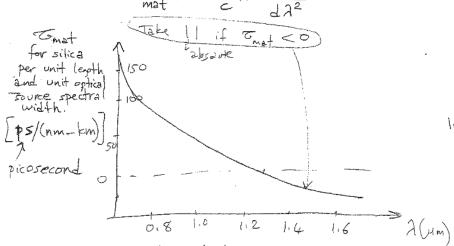
$$= \frac{L}{E} \left[n - \lambda \frac{dn}{da} \right] = \frac{L}{E} N_g$$

Ng = group index

The pulse spread due to material dispersion Ematis

$$G_{\text{mat}} = \frac{d t_{\text{mat}}}{d \lambda} G_{\lambda} = -\frac{L_{\lambda} \left[\frac{d n}{d \lambda} + \lambda \frac{d^{2} n}{d \lambda^{2}} - \frac{d n}{d \lambda} \right]}{d \lambda^{2}}$$

 $\mathcal{E}_{mat} = -\frac{Lf_{1}\lambda}{c} \frac{J^{2}n}{J\lambda^{2}}$

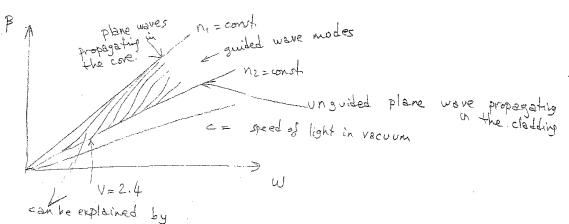


1.54 0.4 1.0 20 (Mm)

- Material dispersion - 0 at 1.27 um for pure silica

Wavequide dispersion

Is due to the explicit dependence of β on ω i.e. $\beta = \frac{\omega}{c} n$, i.e. β varies with ω even though there is no material dispersion (i.e. $n \neq n(\omega)$)



can be explained by

Charact equ. in slab waveguide.

Rx w variations may vary depending on the fiber

variation of K, i.e p in a mode as w varies (W 1 R7)

-> without derivation pulse spread due to waveguide dispersion is:

$$\mathcal{G}_{\text{ug}} = -\frac{n_2 L \Lambda \sigma_{\lambda}}{c \lambda} V \frac{d^2(Vb)}{dV^2}$$

where $b = \frac{P/k - n_2}{N_1 - N_0}$

At shorter " 2 < 1.3 µm, waveguide disprodument of shorter " 2 < 1.3 µm, material " "

20 f

10 f

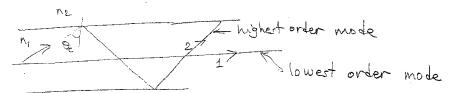
20 f

20

Intermodal Dispersion

Due to the delays occurring between the different modes. In step index fiber

~~



Frod = Tmax - Tmin = L Ng_ L Ng_ group ref. ind. of ray 2

arrival arrival

time of time of lowest order

mode mode

where $N_g = n - \lambda \frac{dn}{d\lambda}$.

If no mat. Lisp. $N_g = n$

$$\frac{1}{2} = \frac{1}{2} \left(n_1 - n_2 \right)$$

-> Tomos dominates pulse spreading in step index fibers.
-> Relative dominance of Smod is greater for laser

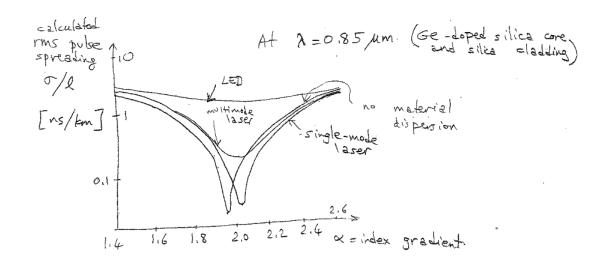
Total rms pulse broadening can be found as $\sigma = \left(\frac{z^2}{\text{intermodal}} + \frac{z^2}{\text{intermodal}}\right)^{1/2}$ where $\sigma_{\text{intermodal}} = \left(\frac{z^2}{z^2} - \frac{z^2}{z^2}\right)^{1/2}$

 $\frac{1}{\sqrt{2}} = \frac{1}{\sqrt{2}} = \frac{1$

Dispersion in graded index fibers

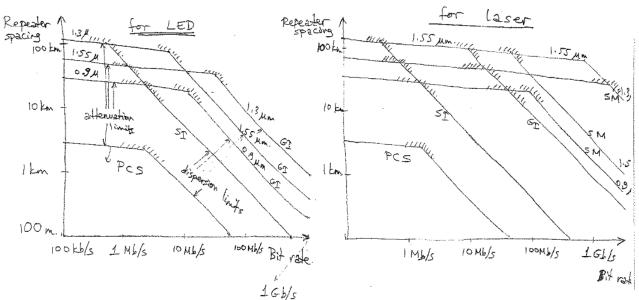
== 2, i've parabolic profile is optimum for low dispersion in graded index fibers.

Low dispersion > high data rate over long distances possible Large core still low dispersion (single-mode filers have low dispersion too, however core is very small, i.e difficulty in splicing)



Optimum Wavelength for Silica Fibers

Here we plot the optimum wavelength curves where the system parameters are the bandwidth and repeater spacing, the fiber properties that determine these system parameters are dispersion and attenuation.



PCS = polymer clad-silica

ST = Step index

ST = 9vaded index

SM = single mode fiber

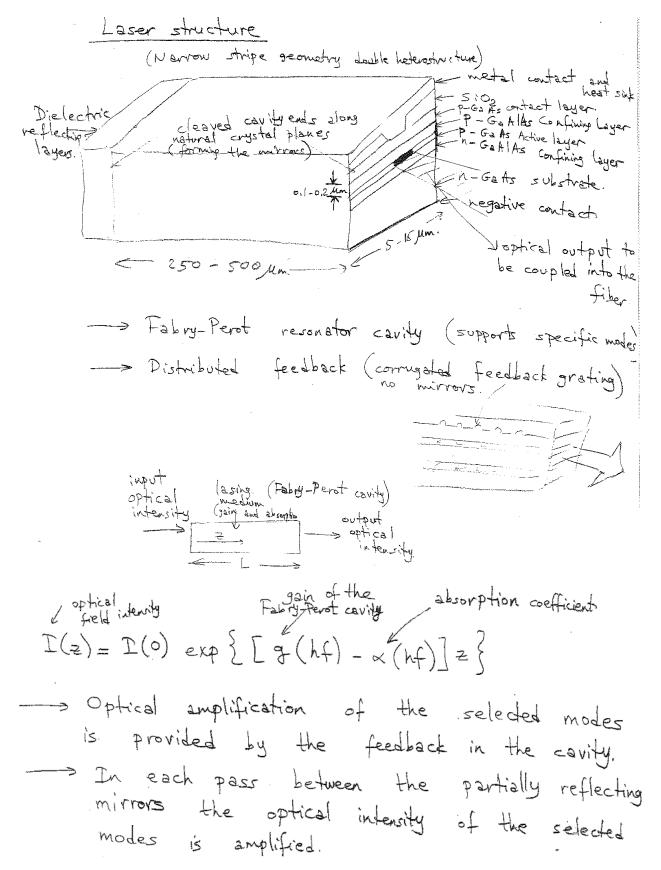
Attenuation is the limiting factor

for low data vates, dispersion is

the limiting factor for high data

vates

7. Optical Sources and Detectors used in Optical Fiber Systems



-> When the gain of the selected modes is sufficient to exceed the optical loss during one roundtrip in the cavity, lasing occurs. For the round trip I (2L) = I(0) R, R2 exp {2L [g(hf) - x(hf)]} reflectivity reflectivity of mirror 2 -> At the lasing threshold I(2L) = I(0) => ie it behaves as an oscillate $g_{\perp h} = (2L)^{-1} \ln \left[(R_1 R_2)^{-1} \right] + \infty$ I gain at threshold (cm) Threshold current density Ith is (i= IthA $J_{th} = \frac{8\pi \ \text{g d} \ \Delta f \ n^2}{\lambda^2 \ \text{l}} g_{th} \qquad (\frac{\Delta m_z}{m^2})$ where d = thickness of the mode confinement volume n = refractive index Ri = internal quantum efficiency. laser power Po (mw) foo Af = transition linewidth for a pulsed semiconductor

Output Power of Semiconductor Lasers

As injection current is increased above threshold laser oscillations build up and the resulting stimulated emission reduces the population inversion until it is clamped at the threshold value is increase the gain anymore but then power the power threshold will not increase the gain anymore but emitted by stimulated emission is

$$P = A \left(J - J_{th}\right) \frac{n_i h f^{1-\frac{1}{2}}}{9}$$

$$\int_{charge}^{2} \int_{charge}^{2} \int_{charge}^{2}$$

(proportional to x) Part of this power is dissipated in the laser cavity and the rest is coupled via the end mirrors (proportional to $(2L)^{-1} \ln \left(R_1 R_2 \right)^{-1}$]

.. Output power is
$$P_{o} = \frac{A \left[J - J_{th} \right] \cdot hf}{q} \frac{\left[\frac{1}{2L} \ln \left(\frac{1}{R_{i}R_{2}} \right) \right]}{\left[x + \frac{1}{2L} \ln \left(\frac{1}{R_{i}R_{2}} \right) \right]} \eta_{i}^{2}$$

- 3 Plot on p. 63

-> External quantum efficiency next.

$$l_{ext} = \frac{q}{E_g} \frac{dP}{di} = 0.8065 \lambda (\mu m) \frac{dP}{di} (m\lambda)$$

1=0,3-0,4 for semiconductor lasers.

Modal Properties of semiconductor lasers

- Transverse modes (spatial modes) depend on the geometry of the optical resonator. Determines the directivity of the laser beam. Each transverse mode has different beam intensity distribution.

- Longitudinal modes (temporal modes) - Due to standing wave patterns formed in the longitudinal direction inside the resonator retractive when the longitudinal direction in the longitud

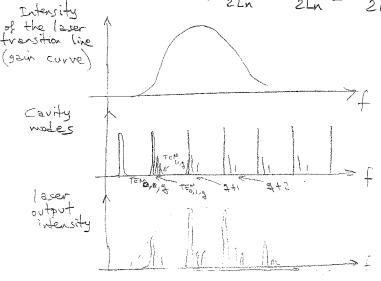
Prop. distance for round trip V=0,1,2...Phase

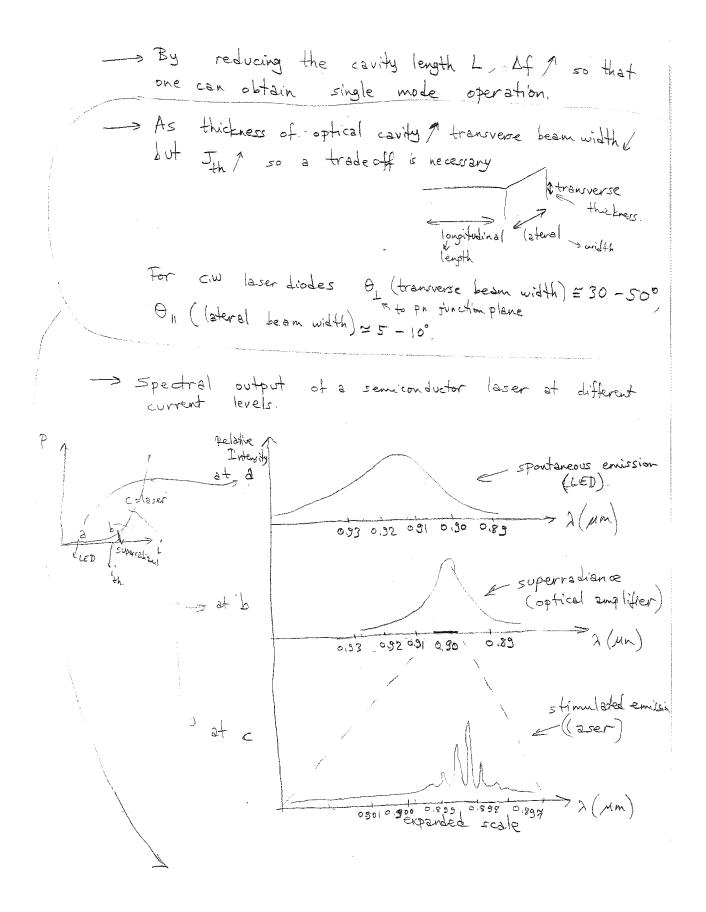
frequency exist of oscillation number (resonator length)

, I may be large its exact value is not important.

Af = frequency separation between axial moder

 $\Delta f = (V+1) \frac{c}{2Ln} - V \frac{c}{2Ln} = \frac{c}{2Ln}$





-> Modulation of laser diodes

Toph = photon lifetime = average time the photon stays in the cavity before being lost either by absorption or by emission.

 $\Delta w = \text{Modulation bandwidth of laser} \propto \frac{1}{\epsilon_{oh}} = \frac{\epsilon_{n}}{n} \epsilon_{hh}$

Since 9th 1 = Jth 1

As Jth 1, DW1 however Jth 1 lifetime 1

In pulse modulation delay time (t) limits the modulation

to a pulse current amplitude rate.

Top + (ib - ith)

lifetime of current current

current

carriers in the recombination region when I = ip + ip is close

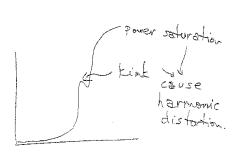
to ith

If the laser is completely turned aff after each pulse, on the onset of a current pulse, a period to is needed to achieve population inversion necessary to produce a gain that is sufficient to overcome the optical losses in the cavity.

-> to is eliminated by choosing is = ith

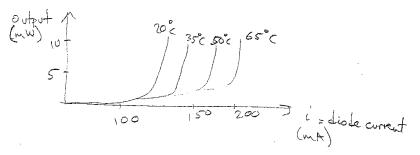
analog modulation

laser PA r in er



Temperature effects

Threshold current depends on temperature. Thus a feedback is needed in laser drive circuitry to stabilize the laser output i.e if a constant optical power level is needed as the temperature of the laser changes or as the laser ages, it is necessary to adjust the dc bias current.



-> Peliability - Operating lifetime (G) & J-n

ourrent

-> As TA - 1.15 \(\)

Faser lifetime also depends on facet degradation.

(could be catastrophic due to mechanical damage to facets
or could erode during some time.)

LED and laser diode performance > Comparison of DLD'S LEDS Testhister of big required not required Bandwidth of the source (rms) 15-60 nm. 2-4 nm. 1-10 mw output power 1-10 mw Power launched 0.5-5 mW 0,03 -0,3mW Rise time, 10-90% ≤ 1 ns 2-20 ns OT = province Modulation 3dh on a lateral >500 MHz < 200 HHZ forward correct 10-300mA 50 -300 mt not required Threshold correct 5-250mA Source coherence Property more colorest more incoherent circular 50 km in 2 ia motor (5 ur foce emitor)
50-70 km (edge emitor)
150 tropic with 120° half power bandwidth (surface emitor)
CII = 120° D1 = 30° (edge emitor) I to pur just plane 5-15 Mm (4) Le eniting sizes emision 8 = 30-55° cost Cho 20

Photodetectors

-- Converts optical power into electric current

-> For optical fiber systems mostly used detectors are the semiconductor pin photodetector and avalanche photodiode (APD).

-> Requirements for a good detector

- high sensitivity (should be able to detect as low power as possible before the noise factor starts to limit the performance), i.e low NEP (noise equivalent power)

of operation of the source)

- Speed (should be fast enough, i.e should have large enough bandwidth to follow the data rate being used).

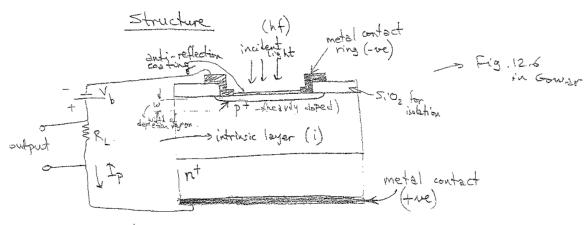
- minimum addition of noise to =ystem

- low cost and long life time

- compatible size to optical fiber dimensions.

- insensitive to temperature variations.

-> Pin photodetector



Operation

- large reverse bias is applied = intrinsic region is

(to improve speed and efficiency) fully depleted of cami

(intrinsic in an and p

<< impurity concentration in(i) region</p>

- Incident photon of energy > Eg of the semiconductor material strikes the p-type material
- Incident photon excites an electron from the valence band to conduction band, generating electron-hole
- High reverse bias separates the electron-hole pairs and collects them across the reverse-biased junction, causing the photocurrent flow through the external
 - The average photocurrent Ip, generated by a steady state average optical power Po is given by

 Ip = 7. (# of electron-hole pairs)

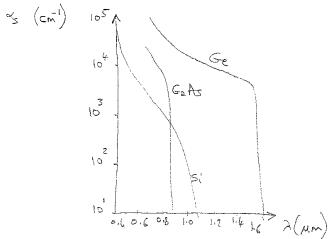
 electron charge

of electron-hole pairs = (Power absorbed in the) x (fraction of the reflecte Power Power)

$$= \frac{P_o\left(1 - e^{-\kappa_s(\lambda)}w\right) \times \left(1 - R_{\mathcal{I}}\right)}{hf}$$

here w = width of the depletion region $R_f = reflectivity$ of the entrance face of the photodial (anti-reflection coating)

 $K_s(\lambda) = absorption$ coefficient of the semiconductor material



$$T_p = \frac{7}{hf} P_o \left(1 - e^{-\kappa_s(A) W} \right) \left(1 - R_f \right)$$

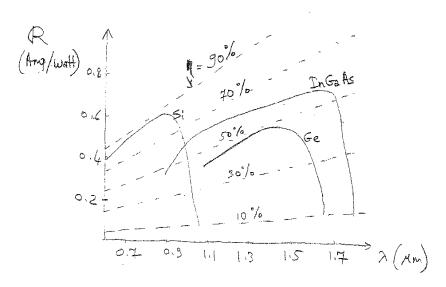
Ruantum Efficiency,
$$n$$
 of the photodetector $n \triangleq \frac{\# \text{ electron-hole Pairs generated}}{\# \text{ incident photons}} = \frac{\text{Tp/q}}{\text{Po/hf}}$
 $n = (1-e^{-\alpha_s(\lambda)w})(1-R_f)$

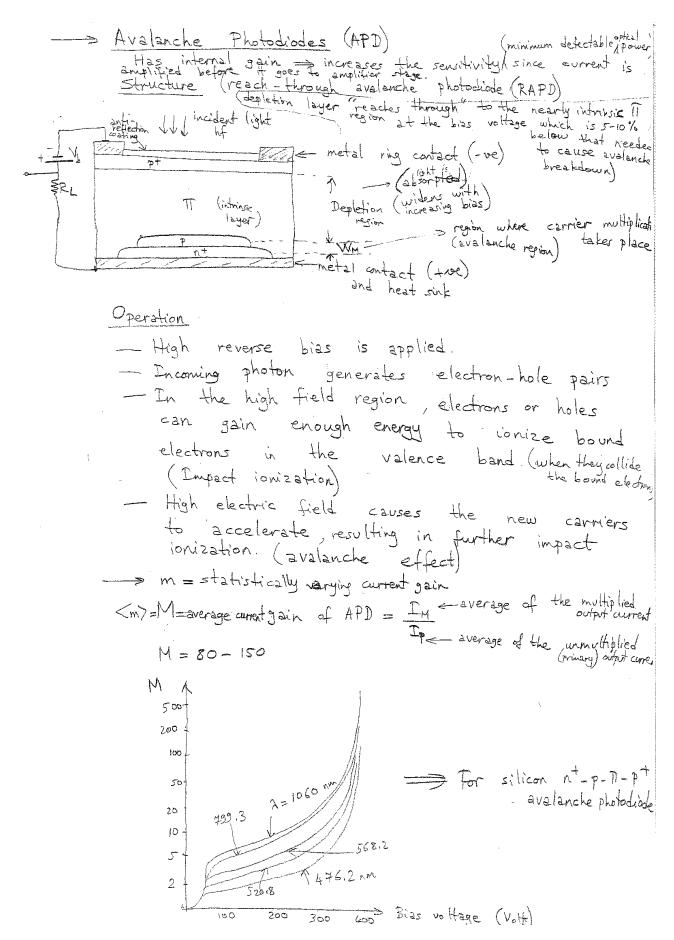
-> As W/, n/ -> depletion layer should be thick so that most of the incident light is absorbed in this region

Responsivity, R of the photodetector

R is defined as the photocurrent generated per unit optical power

$$R \triangleq \frac{I_p}{P_0} = \frac{q}{hf} \eta \neq quantum efficiency.$$





$$\langle i_{\alpha}^{2} \rangle = 2q T_{p} \langle f \rangle M^{2} F(M)$$

Here Ip is the average primary photocurrent where inth=Ip + ip(t)

Mip(t)= MIp + Mip(t)

modulated average (a.c.) of the photocurrent photocurrent for available for a valid iph = 19 P(t) modulated optical power

F(M) = excess noise factor due to the random nature of avalanche current gain

FA < m2 m = random current gain Fig. 1 (see, p. B) Keing the contraction of the contraction rate $M^{2} = M^{2} = 0.85 - 1.0$ for $M = M^{2} = 0.85 - 1.0$ for M =

Dark current noise = bulk dark ownerst noise + surface dark current win

Dark current is the current that flows through the bias circuit in the absence of incident light on the photodetector

Bulk dark current noise power = < 12 results from the thermally generated electrons and holes at the Pr Junction

< 53 >= 29 ID (AF) M2 F(M) unmultiplied bulk dark current (in the order of) Surface dark current noise power = < i25> results from the surface defects, cleanliness, bias voltage surface area. (quard ring structure is used to prevent i'Ds. Ring' shints the leakage current away from the load

<12> = 271(4) 1 surface leakage current not effected by avalanche gain

". $N_D = total$ detector voice power = $\langle i_0^2 \rangle + \langle i_{DS}^2 \rangle + \langle i_{DS}^2 \rangle$ $N_D = 2q (I_p + I_D)(A) M^2 F(M) + 2q I_L(Af)$

 $N_i = N_{R_L} + N_D = \frac{4kT(AF)}{R} + N_D$

 $S_i = \langle [M_{ip}(t)]^2 \rangle = M^2 \langle i_p^2 \rangle$

(SNR) = M2 < 1/2 > 2q (Ip+ID) M2 (A) F(M) + 27 I (M) + 4 K TAF)

-> Generally
-For pin photodiodes Ne dominates No =>
Thus " make the system thermal noise

- For APD, No dominates NR, => Thus APD makes the system quantum noise limited

-> As M/, Sil and also Nol For smaller values of M (but still M >1) (SNR); 1 as M1, i.e it is better to use APD instead of pin photodelector.

However for larger values of M, F(M) becomes very large causing (SNR); to decrease. In this

case it is not advantageous to use APD.

Conclusion is there is an optimum value of M (current gain) in determining whether AFD or pin photodiade is better in terms of noise performance. This optimum M depends not only on the detector parameters (I_L, x, I_D) but also on external parameters (T, RL, Ip). i.e you cannot design an optimum M detector but you can pick an optimum

-> Noise equivalent power = NEP = optical power (of specified 2) required to produce a detector current equal to r.m.s noise current. i'e, NEP = optical power required to make SHR=1. Neglecting thermal noise and surface dark current noise

 $(SNR)_{i} = 1 = \frac{M^{2} < ip^{2}}{2 g (T_{p} + T_{D}) M^{2}(A) F(M)}$

Assume there is no modulation and the signal power=carrier

(ip²) = signal power required to make (CNR); =1 is found as $M^2 \langle p^2 \rangle = 2q \left(I_p + I_D \right) M^2 F(M) M$

 M^2 $ip^2 = M^2 \frac{q}{hf} \frac{p^2}{p}$ since $ip = \frac{qq}{hf} p$ ophical power $ip = \frac{qq}{hf} p$

 $\frac{M^2}{h^2} \left(\frac{nq}{h^2} \right)^2 < P^2 > = 2q \left(I_p + I_D \right) M^2 F(M) (4)$

 $\langle P^2 \rangle = \frac{2q \left(I_p + I_D \right) M^2 F(M) \left(M \right)}{M^2 \left(\frac{nq}{hI} \right)^2}$

optical power to make $(CNR)_{i} = 1$ is $(P^2)_{i} = \sqrt{2q(I_p + I_0)M^2 F(M)W_0^2}$

$$NEP = \frac{\sqrt{\frac{p^2}{hf}}}{\sqrt{Af}} = \frac{\sqrt{\frac{p}{p} + l_D} M^2 F(M)}{R \leftarrow responsivity} = \frac{\sqrt{\frac{\omega a + l_D}{hf}}}{\sqrt{\frac{k}{Hz}}}$$

$$\longrightarrow \text{ Defectivity} = D = \frac{1}{NEP} \left(\frac{He^{1/2}}{w_{a}tt} \right)$$

-> Specific Detectivity = D* \(\text{\text{detectivity}} \) adjusted to be independent of the detector area and bandwith

$$D^* = D A^{1/2}$$
detector
area
$$\left(\frac{cm - H_{=}^{1/2}}{w_{=}^{1/2}}\right)$$

Detector bandwidth (speed)

Depends on:

RC time constant of the photodiode and the amplifier

Photodiode Protodiode series resistance

RT = RL // RA since Rs negligible

- Photocarrier transit time (t) in traversing the depletion Forsi

The state of the strength of the stren Diffusion time of photocarriers generated outside the depletion region.

- Diffusion process is slow compared to drift in the

depletion region

- To have small diffusion time, the photocarriers should be generated in the depletion region or very close to the depletion region. One way of achieving this is to have w large (will also incress From $I_p = \frac{q}{h_L} P_o \left(1 - e^{-\kappa_s w}\right) \left(1 - R_f\right)$ expression one must pick & >> 1 => w >> 1 => x

 $\Rightarrow \text{ If } W \gg \frac{1}{x_s} \text{ and } G = \frac{\epsilon A}{W} \text{ is small } \Rightarrow \text{ high bandwill}$

-> If w> \frac{1}{\pi_s} but G large then bandwidth is determine by I ZTRLC1 - detector cap.

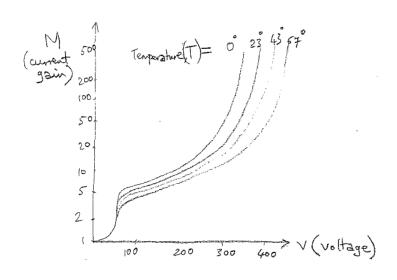
-> As WE Comprome the compromentation of the

-> Also as W & less absorption will take place in the depletion region causing quantum efficiency &

___ Shotty photodiodes ~ 100 GHz is achieved

Temperature effect on avalanche gain

For constant bias voltage as T/ MV. A compensation circuit is needed in the receiver to adjust the bias voltage applied on the photodetector as T changes in order to keep M constant.



Photodiade materials

- In 0.8-0.9 Mm range Si is used most because avalanche multiplication noise Jis small ⇒ high receiver sensitivity and also Si technology is highly developed to Ge, Ga As, InGo As, InGo As P is being used in 0.8-0.9 mm range.

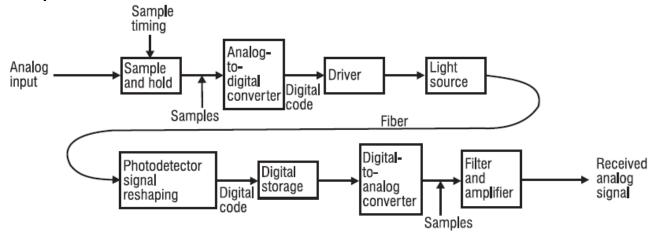
In 1.0 -1.55 μm range Ge is used most since responsivity of Ge in this range is better than Silicon. However Ge has high avalanche multiplication noise, higher dark current.

Also In Go AsP, Go Alsb, In Go As, Go Sb is being used in 1.0-1.6 μm range.

Comparison of pin (Si and Ge) and APD (Si and Ge)

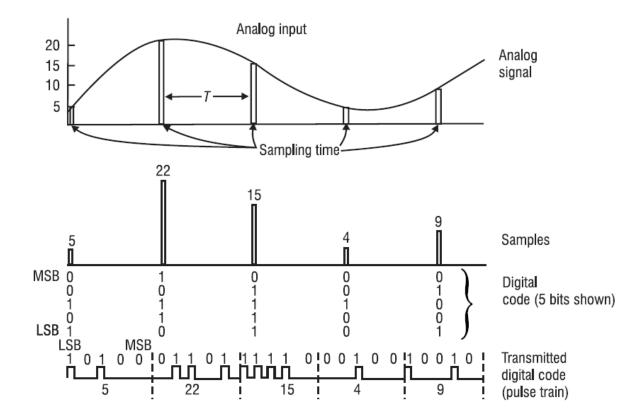
Perform ance Pin APD Germanium Silican 5 Ge 0.4-1.1 7 range (MM) 0,5-1,8 0.4-1.1 0.5-1.65 (= guardum efficience 80 50 80 70 rise time (ns) 0,01 0,3 0,5 reverse bizs voltage(v) 0,25 15 6 170 40 Responsivity (A/W) 0.5 0,7 0.6 6,7 1.0 1.0 80-150 80-150 Sensitivity -35dbm (depends) (10 = 50 db (dependent) 10 - 10 - 11 A dark current $< 10^{-9} \, \text{A}$ cost cheaper expensive

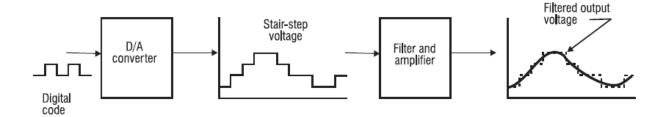
8. Optical Fiber Transmitter



PULSE CODE MODULATION (PCM)

PCM is the conversion of an analog signal into a 2*n*-digit binary code.





An analog signal is placed on the input of a sample and hold.

The sample and hold circuit is used to "capture" the analog voltage long enough for the conversion to take place.

The output of the sample and hold circuit is fed into the analog-to-digital converter (A/D).

An A/D converter operates by taking periodic discrete samples of an analog signal at a specific point in time and converting it to a 2n-bit binary number.

For example, an 8-bit A/D converts an analog voltage into a binary number with 2^8 discrete levels (between 0 and 255).

For an analog voltage to be successfully converted, it must be sampled at a rate at least twice its maximum frequency. This is known as the Nyquist sampling rate.

An example of this is the process that takes place in the telephone system. A standard telephone has a bandwidth of 4 kHz. When you speak into the telephone, your 4-kHz bandwidth voice signal is sampled at twice the 4-kHz frequency or 8 kHz. Each sample is then converted to an 8-bit binary number. This occurs 8000 times per second. Thus, if we multiply 8 k samples/s \times 8 bits/sample = 64 kbits/s, we get the standard bit rate for a single voice channel which is 64 kbits/s.

The output of the A/D converter is then fed into a driver circuit that contains the appropriate circuitry to turn the light source on and off.

The process of turning the light source on and off is known as modulation.

The light then travels through the fiber and is received by a photodetector that converts the optical signal into an electrical current.

A typical photodetector generates a current that is in the micro- or nanoamp range, so amplification and/or signal reshaping is often required.

Once the digital signal has been reconstructed, it is converted back into an analog signal using a device called a digital-to-analog converter or DAC.

A digital storage device or buffer may be used to temporarily store the digital codes during the conversion process.

The DAC accepts an *n*-bit digital number and outputs a continuous series of discrete voltage "steps."

All that is needed to smooth the stair-step voltage out is a simple low-pass filter with its cutoff frequency set at the maximum signal frequency.

DIGITAL ENCODING SCHEMES

Signal format is an important consideration in evaluating the performance of a fiber optic system..

The signal format directly affects the detection of the transmitted signals.

The accuracy of the reproduced signal depends on the intensity of the received signal, the speed and linearity of the receiver, and the noise levels of the transmitted and received signal.

Many coding schemes are used in digital communication systems, each with its own benefits and drawbacks.

The most common encoding schemes are the return-to-zero (RZ) and non-return-to-zero (NRZ).

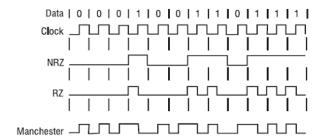
The NRZ encoding scheme, for example, requires only one transition per symbol, whereas RZ format requires two transitions for each data bit.

This implies that the required bandwidth for RZ must be twice that of NRZ. This is not to say that one is better than the other.

Depending on the application, any of the code formats may be more appropriate than the others.

For example, in synchronous transmission systems in which large amounts of data are to be sent, clock synchronization between the transmitter and receiver must be ensured. In this case Manchester encoding is used.

The transmitter clock is embedded in the data. The receiver clock is derived from the guaranteed transition in the middle of each bit.



Format	Symbols per Bit	Self-Clocking	Duty Factor Range (%)
NRZ	1	No	0-100
RZ Manchester	2	No	0-50
(Biphase L)	2	Yes	50

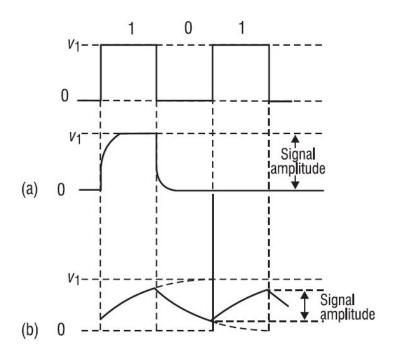
Digital systems are analyzed on the basis of rise time rather than on bandwidth.

The rise time of a signal is defined as the time required for the signal to change from 10% to 90% of its maximum value.

The system rise time is determined by the data rate and code format.

Depending on which code format is used, the number of transitions required to represent the transmitted data may limit the overall data rate of the system.

The system rise time depends on the combined rise time characteristics of the individual system components.

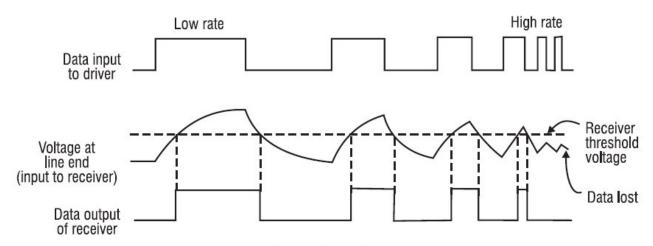


Effect of rise time: (a) Short rise time (b) Long rise time

(a) represents a signal with adequate rise time. Even though the pulses are somewhat rounded on the edges, the signal is still detectable.

In (b) however, the transmitted signal takes too long to respond to the input signal.

The effect is the below figurewhere at high data rates, the rise time limitations cause the data to be distorted and thus lost.



Source: *The TTL Application Handbook*, August 1973f, p. 14-7. Reprinted with permission of National Semiconductor.

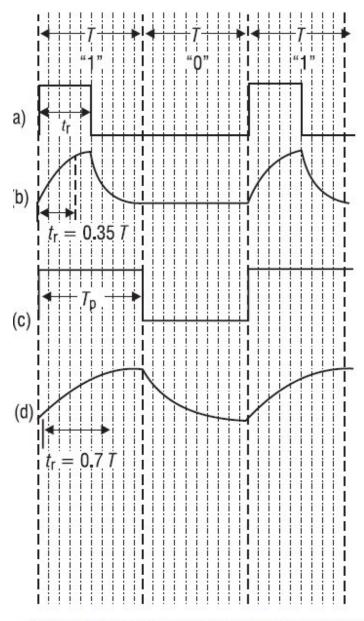
Distortion of data bits by varying data rates

To avoid this distortion, an acceptable criterion is to require that a system have a rise time t_s of no more than 70% of the pulse width T_p , $t_s \le 0.7$ T_p

For an RZ, T_p takes half the bit time T so that $t_s \le 0.7$ T/2 or $t_s \le 0.35/B_r$ where $B_r = 1/T$ is the system bit rate.

For an NRZ format, $T_p = T$ and thus $t_s \le 0.7/B_r$

RZ transmission requires a larger-bandwidth system.



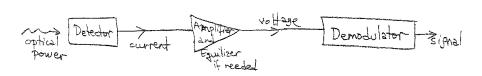
$$T=$$
 Bit time $B_{\rm r}=\frac{1}{T}$ Allowed $t_{\rm r}=$ 0.7 $T_{\rm p}$

Effects of system rise time for RZ format and NRZ format:

- a) Transmitted RZ pulse train
- b) Received RZ signal with allowable tr.
- c) Transmitted NRZ pulse train
- d) Received NRZ pulse train with allowable $t_{\rm r}$

9. Optical Receiver Systems

Draw 38, 430 of Garage Noise Limitation



- Minimum SNR is preset for an acceptable system performing - Minimum average detector current is determined includes 5 to satisfy the SNR requirement the choice) of the or - Minimum detectable optical power is found.

Types of modulation in fiber communication:

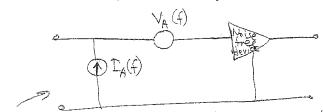
Analog — Direct modulation of optical carrier power by basebard signal.

Modulation — Modulation of the optical carrier power by a frequency modulated subcarrier.

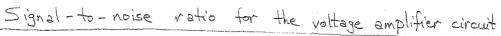
DipHal { - PCM of optical carrier power

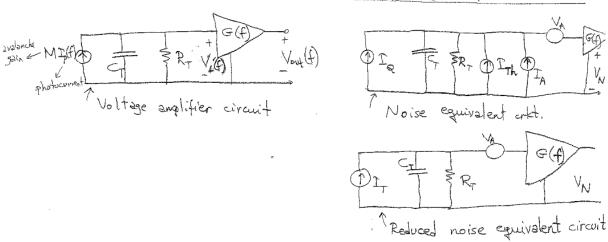
Sources of receiver noise

- _ All the photodetector noises discussed before (quaidum, dark)
- Thermal noise (thermal motion of charge carriers) due to the amplifier input resistance, the bias (load) resistance, and the photodetector resistance
 - _ Active electronic device such as a transistor. The magnitude of this noise depends on the material of the device and its bias.



noise circuit of an active electronic device the voltage source representing voltage per unit bandwidth the current source representing current. Equivalent





where CT= total input capacitance = C_1 + CA

The = provise current of the amplifier per unit bandwilth = \frac{10-14 \text{ A/Hz}}{200-13 \text{ A/Hz}} \times \frac{51-FET}{200-13 \text{ A/Hz}} \times \frac{51-FET}{200-13 \text{ A/Hz}} \times \frac{51-FET}{200-13 \text{ A/Hz}} \times \frac{51-FET}{200-13 \text{ A/Hz}} \times \frac{51-FET}{10-13 \text{ A/Hz}} \times \frac{51-FET}{10-13 \text{ A/Hz}} \times \frac{51-FET}{51-FET} \times \frac{100-13 \text{ A/Hz}}{100-13 \text{ A/Hz}} \times \frac{51-FET}{51-FET} \times \frac{100-13 \text{ A/Hz}}{100-13 \text{ A/Hz}} \times \frac{51-FET}{50-FET} \times \frac{100-13 \text{ A/Hz}}{100-13 \text{ A/Hz}} \times \frac{51-FET}{100-13 \text{ A/Hz}} \time

Voltage $SNR = K = \frac{V_{out}}{V_{N}}$ output noise voltage $SNR = K = \frac{V_{out}}{V_{N}}$

 \rightarrow Output signal vo Hage = Vout (f) = $G(f)V_{i}(f) = G(f)\frac{R_{T}M\dot{I}_{p}(f)}{(1+\dot{J}2\pi fGR)}$

Frequency band of the overall critic that the input signal photocurrent

sees is $\frac{1}{2\pi R_T C_T}$, i.e., the input frequencies above $\frac{1}{2\pi R_T C_T}$ are

bandlimited at the output. In order for all input frequencies (within the signal bandwidth of) to see the same gain, an equalizer is needed, i.e G(f) = Go (1+ = 2TTf C RT) so that Vout = G MRI 16(f) 1 overall output characteristic Imput characteristic Gain characteristic with equalization Total rims output noise power = $V_N = \int |G(f)|^2 V_A^2 df + \int \frac{|G(f)|^2 R_T^2 I_T^2}{|I+j2TIR_TC_i|^2}$ For G(f) = Go (1+ j 2 TT CT PT) VN = G2 SAF { (1+4172f2C2R2) VA2+R2I2 }df Assuming V_A and I_T are independent of frequency in Af $\Rightarrow I_p(f) = I_p$ VN = G. { (1+ 4 T2(Af) 2 CT RT) VA + R2 IT 2 } 1/2 (Af) 1/2 $\frac{1}{V_{N}} = \frac{I_{P}}{V_{N}} = \frac{I_{P}}{\left\{\frac{V_{A}^{2}}{M^{2}}\left(\frac{1}{R_{T}^{2}} + \frac{4\pi^{2}}{3}\left(\Delta f\right)^{2}C_{T}^{2}\right) + 2qI_{P}F(M) + \frac{4kT}{M^{2}R_{T}} + \frac{\Gamma_{A}^{2}V_{A}^{2}}{M^{2}}AV^{2}}\right\}}$

Here Af is the modulation bandwidth. In direct modulation Af is the baseband frequencies, in FM subcarrier systems of extends over

the range of frequency modulation. In PCM, Df=(Bit rate)/2 -> K determines the quality of the communication channel and in system design minimum K is always specified. -20 log K K > 12 => SNR > 21.6 dB K > 200 => SNR > 46 dB for analogue channel. -> Features of K in guiding the general design of the system and evaluating its expected performance: - Initially, as M/ K/ until the quantum (shot) noise term (e) dominates other terms. Thus, there is an optimum M=Mopt above which KK (ie it is not always advantageous to use APD) — If terms (2) and (d) are significant, I in R_T ⇒ I in K. However high RT brings some problems like the need for equalization and the reduction in the dynamic range of the - If Of is large term (b) dominates. Thus Cy should be minimized. I in C7 2/50 K in the equalization amount readed - Term (c) (quantum noise) to be dependent on the level of the received signal. This is a distinguished feature of optical communication systems as - Even though quantum noise is Poisson distributed, in obtaining K, it is assumed that all noise sources are uncorrelated Gaussian The Ideal Case (i.e quantum noise (shot noise) limited M sufficiently large so that term (c) dominates $K = \frac{I_p}{(2q I_p F(M) \Delta f)^{1/2}} \Rightarrow I_p > 2q F(M) K^e \Delta f$ $= \frac{I_p}{R_{APP}} = \frac{I_p}{R_{APP}} =$ minimum rec. power for quantum limited corresponds to Po in detector section operation

-> High Input Peristance Amplifier (Integrating Amplifier)

If terms (2) and (d) in the SNR expression are dominating over others (i.e the thermal noise and amplifient noise voltage are high) then if RTA the receiver can be made shot noise limited. But increasing RT causes integration of the signal (i.e rec bandwidth=1200 equalization becomes necessary. Also for RT large dynamic If RT is large

$$K = \frac{T_{p}}{\frac{\{ \frac{V_{A}^{2}}{M^{2}} \frac{4\pi^{2}}{3} (\Delta f)^{2} c_{r}^{2} + 2q I_{p} F(M) + \frac{T_{A}^{2}}{M^{2}} \}^{1/2} (\Delta f)^{1/2}}}{\frac{(b)}{Define} (\Delta f) \triangleq \frac{\sqrt{3}}{2\pi C_{r}} \frac{I_{A}}{V_{A}}}$$

Signal bandwith (A) needed for quantum noise limited operation (ideal (i.e conditions for term (c) dominating other terms) case

$$\rightarrow If \Delta f < (\Delta f) = term (e) > term(b) so term (e)$$
donninates when $2qI_pF(M) > \frac{I_A}{M^2}$

At quantum noise limited operation $I_p = 2q F(M) K^2 Af$ found before (3)

Subst. (3) into (2)
$$\left(2q F(M) K\right)^2 \Delta f > \frac{\Gamma_A^2}{M^2} \implies \Delta f > \frac{\Gamma_A^2}{\left(2q F(M) K M\right)^2} = \Delta f$$

The Def
$$>$$
 (Def) $=$ 50 term(b) dominates term (e) so term(c) dominates when $2q \operatorname{Ip} F(M) > \frac{V_A^2}{M^2} \frac{4T^2}{3} (\Delta f)^2 C_7^2 = 6$

At quantum limited operation Ip is given by (3) Subst. (3) into (6) we have

$$\Delta f < \frac{3(q MF(M) K)^2}{(\pi C_1 V_A)^2} = (\Delta f)_2$$

$$\longrightarrow$$
 50 if (Δf) , $<\Delta f<(\Delta f)_2$ then we have quantum limited operation. Eq. \bigoplus

With APD, both Si-FET and Si-BJT permit quantum noise limited operation over most practical frequencies.

Low Input Resistance Amplifier

If $\frac{1}{2TRC} > \Delta f \implies R < \frac{1}{2TC\Delta f}$, then no equalization is needed. If $R < \frac{1}{2TC\Delta f}$, then from SNR expression, it can be found that if

$$\frac{V_A^2}{4kT} < R < \frac{4kT}{T_A^2}$$
 (8)

then thermal noise (term d) exceeds amplifier noise (term ande) In addition to (8) if quantum noise (term c) exceeds thermal noise (term d), i.e.

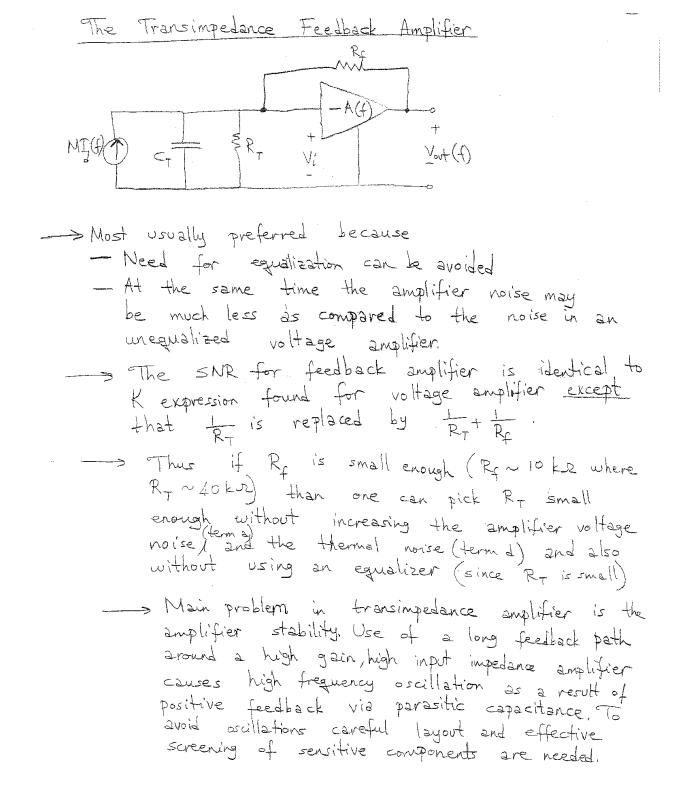
$$2q T_p F(M) > \frac{4kT}{M^2R} = \frac{8T kTC\Delta f}{M^2} \qquad -- (3)$$

then the operation will be quantum limited (best among those could be achieved)

Minimum quantum noise limited current is given by 3

Using 3 in 9 we have
$$C_{f} < \frac{(4MF(M)K)^{2}}{2TkT}$$

A good APD ensures quantum noise limited operation even with a low resistance and no equalization voltage amplifien

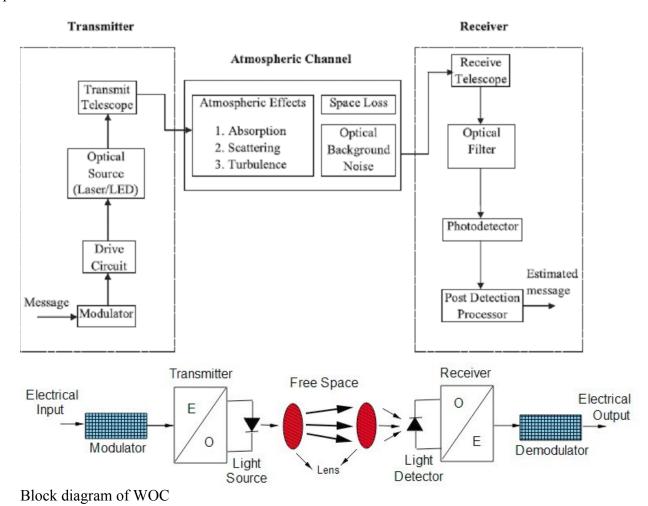


10. Introduction to Free Space Optics (FSO) Systems

Based on their transmission range, WOC (Wireless Optical Communication) can be classified into five broad categories:

(i) Ultrashort-range WOC – used in chip-to-chip communication or all optical lab-on-a-chip system.

- (ii) Short-rangeWOC used in wireless body area networks (WBANs) or wireless personal area networks (WPANs).
- (iii) Medium-range WOC used in indoor IR or visible light communication (VLC) for wireless local area networks (WLANs) and inter-vehicular and vehicle-to-infrastructure communications.
- (iv) Long-range WOC used in terrestrial communication between two buildings or metro area extensions.
- (v) Ultra-long-range WOC used in ground-to-satellite/satellite-to-ground or inter-satellite link or deep space missions.





FSO applications:

• Telecommunication and computer networking

- Point-to-point LOS links
- Temporary network installation for events or other purpose as disaster recovery
- For communications between spacecraft, including elements of satellite constellation
- Security applications
- Military application: (its potential for low electromagnetic emanation when transferring sensitive data for air forces)
- Metro network extensions: carriers can deploy FSO to extend existing metropolitan area fiber rings, to connect new networks, and, in their core infrastructure, to complete SONET rings.
- Enterprise connectivity: the ease with which FSO links can be installed makes them a natural for interconnecting local area network segments that are housed in buildings separated by public streets or other right-of-way property.
- Fiber backup: FSO may also be deployed in redundant links to backup fiber in place of a second fiber link
- Backhaul: FSO can be used to carry cellular telephone traffic from antenna towers back to facilities wired into the public switched telephone network.
- Service acceleration: FSO can be also used to provide instant service to fiber-optic customers while their fiber infrastructure is being laid.
- Last-Mile access: In today's cities, more than 95% of the buildings do not have access to the fiber optic infrastructure due to the development of communication systems after the metropolitan areas. FSO technology seems a promising solution to the connection of endusers to the service providers or to other existing networks. Moreover, FSO provides highspeed connection up to Gbps, which is far more beyond the alternative systems.

FSO Advantages:

- Long distance up to 8 km.
- High bit rates speed rates: the high bandwidth capability of the fiber optic of 2.5 Gbps to 10 Gbps achieved with dense wavelength division multiplexing (DWDM). Modern systems can handle up to 160 signals and can thus expand a basic 10 Gbit/s system over a signal fiber pair to over 1.6 Tbit/s.
- Immunity from electromagnetic interference: secure cannot be detected with RF meter or spectrum analyzer, very narrow and directional beams
- Invisible and eye safe, no health hazards so even a butterfly can fly unscathed through a beam
- Low bit error rates (BER)
- Absence of side lobes
- Deployment of FSO systems quickly and easily
- Low maintenance (Practical)
- Lower costs as compared to fiber networks (FSO costs are as low as 1/5 of fiber network costs).
- License-free long-range operation (in contrast with radio communication)

FSO disadvantages:

For terrestrial applications, the principal limiting factors are beam dispersion, atmospheric absorption, rain, fog, snow, interference from background light sources (including the sun), shadowing, pointing stability in wind, and pollution.

Atmospheric effects:

Transmitted power of the emitted signal is highly affected by scattering, absorption and turbulence.

Attenuation is the result of absorption and scattering by molecules and particles (aerosols) suspended in the atmosphere.

Distortion, on the other hand, is caused by atmospheric turbulence due to random index of refraction fluctuations.

Attenuation affects the mean value of the received signal in an optical link whereas distortion results in variation of the signal around the mean.

Aerosols:

Aerosols are particles suspended in the atmosphere with different concentrations. Each aerosol cause absorption and scattering.

They have diverse nature, shape, and size. Aerosols can vary in distribution, constituents, and concentration. As a result, the interaction between aerosols and light can have a large dynamic, in terms of wavelength range of interest and magnitude of the atmospheric scattering itself. Some aerosols are rain, smoke, fog, snow, desert dust particles, human-made industrial particulates, maritime droplets.

Aerosol scattering are explained by Mie scattering theory because the sizes of aerosols are comparable to or larger than the wavelength of the optical communications.

Transmitted optical beams in free space are attenuated most by the fog and haze droplets mainly due to dominance of Mie scattering and absorption effects in the wavelength band of interest in FSO (0.5 μ m – 2 μ m).

The Mie scattering coefficient is

$$\beta_{a(scat)} = \alpha_a N_a$$
 in 1/km

where α_a is the Mie scattering cross-section in km² and N_a is the number density of air particles in $1/\text{km}^3$.

An aerosol's concentration, composition and dimension distribution vary temporally and spatially varying, so it is difficult to predict attenuation by aerosols. Although their concentration is closely related to the optical visibility, there is no single particle dimension distribution for a given visibility. Due to the fact that the visibility is an easily obtainable parameter, either from airport or weather data, the scattering coefficient $\beta_{a(scat)}$ is expressed as

$$\beta_{a(scat)} = \left(\frac{3.91}{V}\right) \left(\frac{0.55}{\lambda}\right)^{i}$$

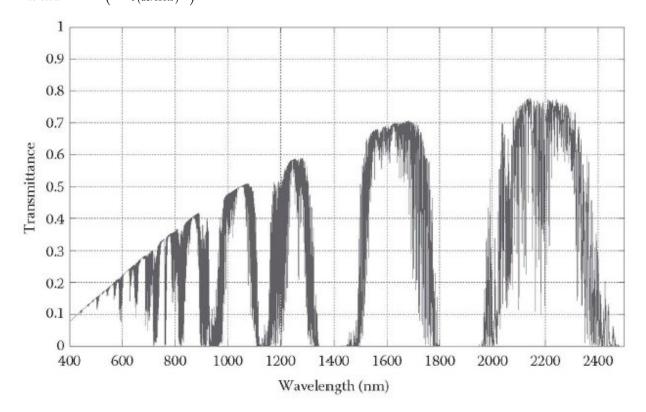
where V is the visibility (Visual Range) in km, λ is the incident laser beam wavelength μ m, i is the size distribution of the scattering particles which typically varies from 0.7 to 1.6 corresponding to visibility conditions from poor to excellent.

Also the absorption coefficient of the aerosol $\beta_{a(absorp)}$ is found and the atmospheric transmittance due to an aerosol is found to be

$$\tau_{aerosol} = \exp(-\beta_{T(aerosol)}L)$$

where the total attenuation due to an aerosol is $\beta_{T(aerosols)} = \beta_{a(scat)} + \beta_{a(absorp)}$ and L is the link distance, i.e., the distance between from the transmitter and the receiver.

Thus, the total attenuation due to aerosols is found by evaluating the scattering and absorption coefficients of each aerosol present in the FSO link and by adding them to find $\beta_{T(aerosols)}$ and $\tau_{aerosols} = \exp(-\beta_{T(aerosols)}L)$.



Atmospheric transmittance window with absortion contribution.

Molecules:

There are more than 40 different molecules in the atmosphere, e.g., nitrogen, hydrogen, carbon dioxide, ... etc. Each of these molecules cause scattering and absortion.

Rayleigh (molecular) scattering refers to scattering by molecular and atmospheric gases of sizes much less than the incident light wavelength. The Rayleigh scattering coefficient is given by

$$\beta_{m(scat)} = \alpha_m N_m \text{ in } 1/\text{km}$$

where α_m is the Rayleigh scattering cross-section in km², N_m is the number density of air molecules in 1 /km³.

Rayleigh scattering cross section is inversely proportional to fourth power of the wavelength of incident beam (λ^{-4}) as

$$\alpha_{m(scat)} = \frac{8\pi^3 (n^2 - 1)^2}{3N^2 \lambda^4} \text{ in km}^2$$

where n is the index of refraction, λ is the incident light wavelength in m, N is the volumetric density of the molecules in $1/\text{km}^3$.

The result is that Rayleigh scattering is negligible in the infrared waveband because Rayleigh scattering is primarily significant in the ultraviolet to visible wave range.

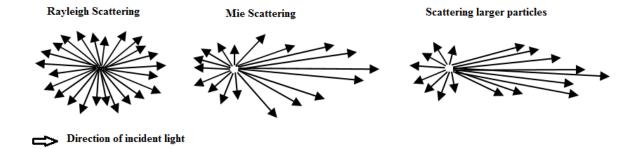
Also the absorption coefficient of the molecule $\beta_{m(absorp)}$ is found and the atmospheric transmittance attenuation due to a molecule is found to be

$$\tau_{molecule} = \exp(-\beta_{T(molecule)}L)$$

where the total attenuation due to a molecule is $\beta_{T(molecule)} = \beta_{m(scat)} + \beta_{m(absorp)}$ and L is the link distance, i.e., the distance between from the transmitter and the receiver.

Thus, the total attenuation due to molecules is found by evaluating the scattering and absorption coefficients of each molecule present in the FSO link and by adding them to find $\beta_{T(molecules)}$ and

$$\tau_{molecules} = \exp(-\beta_{T(molecules)}L).$$



<u>Turbulence</u>

Clear air turbulence phenomena affect the propagation of optical beam by both spatial and temporal random fluctuations of refractive index due to temperature, pressure, and wind variations along the optical propagation path.

Atmospheric turbulence primary causes phase shifts of the propagating optical signals resulting in distortions in the wave front.

These distortions, referred to as optical aberrations, also cause intensity distortions, referred to as scintillation.

Moisture, aerosols, temperature and pressure changes produce refractive index variations in the air by causing random variations in density.

These variations are referred to as eddies and have a lens effect on light passing through them.

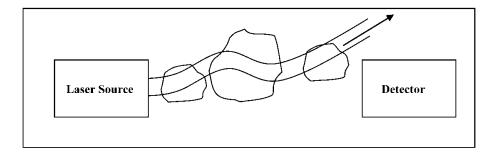
When the light beam wave passes through these eddies, parts of it are refracted randomly causing a distorted wave front with the combined effects of variation of intensity across the wave front and warping of the isophase surface.

As the result, turbulence causes scattering $\tau_{turbulence} = \exp(-\beta_{t(scat)}L)$

i.e., the overall total attenuation due to aerosols, molecules and turbulence is found by $\beta_{T(overall)} = \beta_{a(scat)} + \beta_{a(absorp)} + \beta_{m(scat)} + \beta_{m(absorp)} + \beta_{t(scat)} \text{ and } \tau_{overall} = \exp(-\beta_{T(overall)}L).$

Other effects of turbulence:

Beam wander



- Beam spread: Beam size at the receiver is increased further on top of free space diffraction.
- Intensity fluctuations: Intensity at the receiver fluctuates in time and space.

11. Propagation of Light in FSO

Free-Space Propagation of Gaussian-Beam Waves

The mathematical description of a propagating wave involves a field.

Basically, a field $u(\mathbf{R},t)$ is a function of space $\mathbf{R} = (x, y, z)$ and time t that satisfies a partial differential equation.

In the case of electromagnetic radiation, the field may be a transverse electromagnetic (TEM) wave, whereas for acoustic waves the field may represent a pressure wave.

The governing equation in most cases is the wave equation

$$\nabla^2 u = \frac{1}{c^2} \frac{\partial^2 u}{\partial u^2}$$

where $c = 3 \times 10^8$ m/s is the speed of the propagating wave which is light and ∇^2 is the Laplacian operator defined in rectangular coordinates by

$$\nabla^2 u = \frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} + \frac{\partial^2 u}{\partial z^2}.$$

If we assume that time variations in the field are sinusoidal (i.e., a monochromatic wave), then we look for solutions of the form $u(\mathbf{R},t) = U_0(\mathbf{R})e^{-i\omega t}$ where ω is the angular frequency and $U_0(\mathbf{R})$ is the complex amplitude of the wave which is the spatial field.

The substitution of this solution form into the wave equation leads to the time-independent reduced wave equation (or Helmholtz equation)

 $\nabla^2 U_0 + k^2 U_0 = 0$ where k is the optical wave number related to the optical wavelength λ by $k = \omega/c = 2\pi/\lambda$.

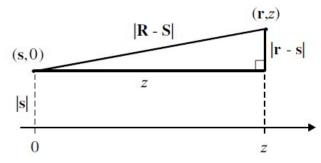
For optical wave propagation, Helmholtz equation can be further reduced to what is called the paraxial wave equation.

Let us assume the beam originates in the plane at z=0 and propagates along the positive z-axis. If we also assume the free-space optical field at any point along the propagation path remains rotationally symmetric, then it can be expressed as a function of $r = \sqrt{x^2 + y^2}$ and z.

Thus, the reduced wave equation in cylindrical coordinates can be written as

$$\frac{1}{r}\frac{\partial}{\partial r}\left(r\frac{\partial U_0}{\partial r}\right) + \frac{\partial^2 U_0}{\partial r^2} + k^2 U_0 = 0$$

Paraxial approximation can be made when the propagation distance of an optical wave along the *z*-axis is much greater than the transverse spreading of the wave.



If $\mathbf{R} = (\mathbf{r}, z)$ and $\mathbf{S} = (\mathbf{s}, z)$ denote two points in space with \mathbf{r} and s transverse to the propagation axis, then the distance between such points is

$$|\mathbf{R} - \mathbf{S}| = (z^2 + |\mathbf{r} - \mathbf{s}|^2)^{1/2} = z \left(1 + \frac{|\mathbf{r} - \mathbf{s}|^2}{z^2}\right)^{1/2}$$

If the transverse distance is much smaller than the longitudinal propagation distance between the points, then the second factor can be expanded in a binomial series to obtain

$$\left|\mathbf{R} - \mathbf{S}\right| = z \left(1 + \frac{\left|\mathbf{r} - \mathbf{s}\right|^2 + \dots}{2z^2}\right) = z + \frac{\left|\mathbf{r} - \mathbf{s}\right|^2}{2z} + \dots, \quad \left|\mathbf{r} - \mathbf{s}\right| << z \quad \text{which is known as the paraxial approximation.}$$

The complex amplitude at propagation distance z from the source is given by Huygens-Fresnel integral as

$$U(\mathbf{r},z) = -2ik \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} G(\mathbf{s},\mathbf{r};z) U_0(\mathbf{s},0) d^2s$$

where $U_0(\mathbf{s},0)$ is the optical wave at the source plane and $G(\mathbf{s},\mathbf{r};z)$ is the free-space Green's function which can be expressed under the paraxial approximation as

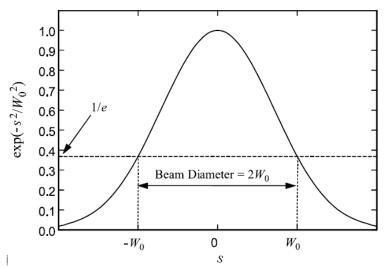
$$G(\mathbf{s}, \mathbf{r}; z) = \frac{e^{ik} |\mathbf{R} - \mathbf{S}|}{4\pi |\mathbf{R} - \mathbf{S}|} \cong \frac{1}{4\pi z} \exp\left(ikz + \frac{ik}{2z} |\mathbf{r} - \mathbf{s}|^2\right)$$

The complex amplitude of the Gaussian-beam wave at the source plane z=0 is

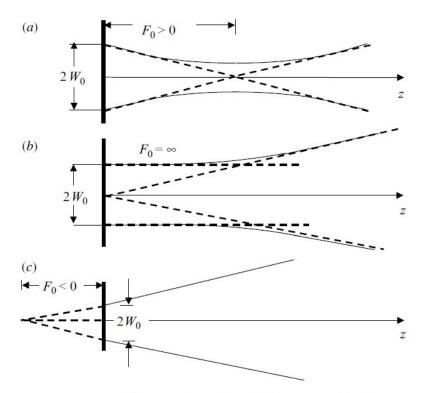
$$U_0(\mathbf{s},0) = A \exp\left(-\frac{1}{2}\alpha_0 k s^2\right) = A \exp\left[\frac{ik}{2z}(i\alpha_0 z) s^2\right] = A \exp\left[-\frac{s^2}{W_0^2} - \frac{ik}{2F_0} s^2\right]$$

where A is the amplitude at the origin, $s = \sqrt{x^2 + y^2}$ is radial distance from the beam center line and $\alpha_0 = \frac{2}{kW_0^2} + i\frac{1}{F_0}$. It is assumed that the transmitting aperture is located in the plane z=0 and the amplitude distribution in this plane is Gaussian with effective beam radius (spot size) W_0 in meters, which denotes

distribution in this plane is Gaussian with effective beam radius (spot size) W_0 in meters, which denotes the radius at which the field amplitude falls to 1/e of that on the beam axis as shown below for A=1



Additionally, the phase front is taken to be parabolic with radius of curvature F_0 in meters. The particular cases $F_0 = \infty$, $F_0 > 0$, $F_0 < 0$ correspond to collimated, convergent, and divergent beam forms, respectively



(a) Convergent beam, (b) collimated beam, and (c) divergent beam. Thus, for the Gaussian beam, Huygens-Fresnel integral becomes

$$U(\mathbf{r},z) = -2ik \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \frac{1}{4\pi z} \exp\left(ikz + \frac{ik}{2z} |\mathbf{r} - \mathbf{s}|^2\right) A \exp\left[\frac{ik}{2z} (i\alpha_0 z) s^2\right] d^2 s$$

Changing the integration to polar coordinated where $d^2s = sd\theta ds$ and rearranging

$$U(\mathbf{r},z) = -\frac{Aik}{2\pi z} \exp\left(ikz + \frac{ik}{2z}r^2\right) \int_{0}^{\infty} \int_{0}^{2\pi} \exp\left(-\frac{ik}{z}rs\cos\theta\right) \exp\left[\frac{ik}{2z}(1+i\alpha_0z)s^2\right] sd\theta d^2s$$

Performing the integrations, the electric field at the receiver is found as

$$U(\mathbf{r},z) = \frac{A}{1+i\alpha_0 z} \exp\left[ikz + \frac{ik}{2z} \left(\frac{i\alpha_0 z}{1+i\alpha_0 z}\right)r^2\right]$$

The intensity at the receiver is $I(\mathbf{r},z) = U(\mathbf{r},z)U^*(\mathbf{r},z)$

12. FSO Link Design

The ability for an optical link to deliver the signal power to the receiver is governed by the link equation

$$P_{R} = P_{T} \left(\eta_{T} \eta_{A} \frac{4\pi A_{T}}{\lambda^{2}} \right) L_{TP} L_{atm} L_{pol} L_{RP} \left(\frac{A_{R}}{4\pi z^{2}} \right) \eta_{R}$$

where

 P_R is the total signal power at the input to the receiver. For the uplink, this is defined at the input to the optical detector. For the downlink, the receive signal power is defined at the input to the receive optical detector.

 P_{T} is the transmit optical power at the transmit interface,

 η_T is the transmit optics efficiency,

 $\eta_{\scriptscriptstyle A}$ is the aperture illumination efficiency of the transmitter lens,

 λ is the wavelength,

 A_T is the aperture area,

 L_{TP} is the transmitter pointing loss, defined as the ratio of power radiated in the direction of receiver to the peak radiated power. If the transmitter is directly pointed at the receiver, the pointing loss is 0 dB,

 L_{atm} is the fractional loss due to absorption of the medium (e.g., earth atmosphere),

 L_{pol} is the fractional signal loss due to mismatch of the transmitting and receiving polarization patterns,

 L_{RP} is the receiver pointing loss, defined as the ratio of receiving lens gain in the direction of the transmitting lens to the peak receiving lens gain,

 A_R is the receive aperture area,

z is the link distance,

the term $\left(\frac{A_R}{4\pi z^2}\right)$ is the fraction of power that is collected by the receiving aperture if the transmitter is an

isotropic radiator.

 η_R is the receiving optics collecting efficiency, defined as the fraction of optical power at the receiving aperture that is collected within the field of view of the receive detector.

Thus, the receive signal power can be improved by the following:

- 1) Increasing the transmit power. The most straightforward method of improving the receive signal power is to increase the power at the transmitter since the receive power scales linearly with the transmit power. However, increasing the transmit power also increases the overall system power consumption which, for a deep-space mission, is typically at a premium. Furthermore, the increased power consumption can lead to thermal management issues (increased radiator size and hence mass) for the host spacecraft, as well as reliability concerns.
- 2) Increasing the transmit aperture. This effectively reduces the transmit beamwidth and hence improves the power delivery efficiency. However, the pointing and tracking of the narrow downlink becomes increasingly more difficult with a narrower downlink. Furthermore, the aperture size is highly correlated with the mass of the transmit terminal and hence cannot be increased indefinitely.
- 3) Reducing the operating wavelength. Reducing the operating wavelength reduces the diffraction loss of the signal (i.e., reduces the transmit beamwidth). However, the wavelength selection is strongly constrained by the available laser technology, as well as considerations on the receiver sensitivity and detector technology. Furthermore, the transmittance of the atmosphere also depends on the wavelength, as well as the amount of sky background irradiance.
- 4) Increasing the receiver aperture area. Since the receive signal power scales linearly with the receive aperture area, increasing the receiver aperture area is a relatively simple way to improve the system performance. However, for daytime operations of a receiver inside the Earth's atmosphere, the amount of background noise collected also increases with increasing receiver aperture, and the effective performance improvement does not always scale linearly with increasing aperture area.

- 5) Reduced pointing loss. Reducing the pointing loss improves the overall signal energy and also reduces the point-induced signal power fluctuation.
- 6) Improving the overall efficiency, including transmit and receive optical loss, and polarization mismatch losses. This generally requires attention to the optical design. Of particular attention is the transmit optics design. The transmit aperture illumination efficiency, η_A , depends on the phase and intensity distribution over the aperture. For the general case of a transmit aperture being illuminated by a Gaussian beam, the aperture illumination efficiency can be written as:

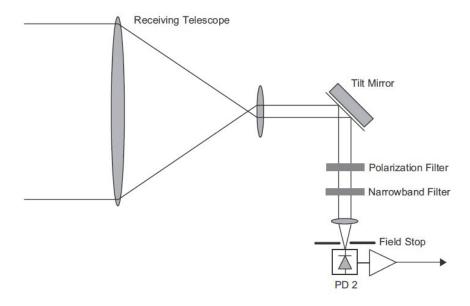
$$\eta_A = \frac{2S}{\alpha^2} \left[\exp\left(-\alpha^2 \gamma^2\right) - \exp\left(-\alpha^2\right) \right]^2$$

where α is the ratio between the aperture diameter and the Gaussian beam $(1/e^2)$ diameter of the transmit signal, γ is the obscuration ratio (darkening ratio) and S is the Strehl ratio, which is defined as the intensity at the center of the aberrated system to that of an ideal optical system.

Optical-Receiver Sensitivity

In addition to the effective delivery of the signal to the detector, the performance of the optical link also depends on the receiver sensitivity (measured in terms of received photons per bit). Because of the high cost associated with increasing the transmit power and system aperture, improving the receiver sensitivity is an important factor

In a direct-detection receiver, the received optical intensity is detected without extensive front-end optical processing.



The incident signal is collected by the receive telescope. A polarization filter followed by a narrowband filter, and a field stop effectively reduces the amount of background noise incident onto the detector.

The capacity of a direct detention optical channel in the presence of background can be written as:

$$C = \left(\log_2 e\right) \frac{\lambda_s}{M} \left[\left(1 + \frac{1}{\rho}\right) \ln\left(1 + \rho\right) - \left(1 + \frac{M}{\rho}\right) \ln\left(1 + \frac{\rho}{M}\right) \right]$$

Photon Detection Sensitivity

Improving the photon detection efficiency is an obvious method of improving the channel performance. For a direct-detection receiver, this is generally accomplished by using detectors with internal amplifications, such as avalanche photodiodes (APDs) and photomultiplier tubes (PMTs).

Modulation Format

One practical modulation format to achieve high peak-to-average-power ratio is the M-ary pulse-position modulation (PPM). In an M-ary PPM modulation scheme, each channel symbol period is divided into M time slots, and the information is conveyed through the channel by the time window in which the signal pulse is present.

Link Availability

The communications link budget or the DCT is a useful tool in estimating the physical layer link performance (e.g., the link bit error rate). An operational communications link, on the other hand, must also address the issue of link availability. Overall link availability is aimed at >90 percent depending on the link type. In some links, 99.999 % availability may be required.

Beam Pointing and Tracking

Due to the narrow transmit beamwidth, accurate pointing acquisition and tracking are critical to the deepspace laser communications system implementation.

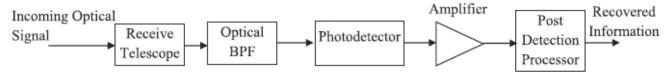
Typical design parameters considered in an FSO link design:

Link Budget	Parameters
Received signal power	Operating wavelength
	Link distance
	Transmit power
	Transmit aperture area
	Transmit optics efficiency
	Transmit Strehl ratio
	Transmit pointing loss
	Polarization mismatch loss
	Receiver aperture area
	Receive optics efficiency
	Receiver detector field of view
	Receiver pointing loss
	Atmospheric attenuation loss
	Scintillation-induced loss
Received background	
power	Receive aperture area

Receive optics efficiency		
Detector field of view		
Receive optical bandwidth		
Background spectral irradiance		
Receive optics scattering behavior		
Detector dark count		

Receiver sensitivity	Detector quantum efficiency
	Detector noise characteristics
	Dark count rate or
	• Detector Excess and thermal
	noise
	Modulation format
	Coding scheme

Direct Detection System



Block diagram of a direct detection scheme

In direct detection technique, the received optical signal is passed through optical band-pass filter to restrict the background radiation.

It is then allowed to fall on the photodetector which produces the output electrical signal proportional to the instantaneous intensity of the received optical signal.

It may be regarded as linear intensity to current convertor or quadratic (square law) converter of optical electric field to detector current.

The photodetector is followed by an electrical low-pass filter (LPF) with bandwidth sufficient enough to pass the information signal.

The signal-to-noise ratio (SNR) of direct detection receiver can be obtained by using noise models for a particular detector, i.e., PIN or avalanche photodetector (APD).

With the received power as given above by

$$P_{R} = P_{T} \left(\eta_{T} \eta_{A} \frac{4\pi A_{T}}{\lambda^{2}} \right) L_{TP} L_{atm} L_{pol} L_{RP} \left(\frac{A_{R}}{4\pi z^{2}} \right) \eta_{R}$$

and detector noise sources, the SNR expressions are obtained for PIN photodetector to be

$$SNR = \frac{\left(R_{0}P_{R}\right)^{2}}{2qB\left(R_{0}P_{R} + R_{0}P_{B} + I_{d}\right) + 4K_{B}TB/R_{L}}$$

where B is the receiver bandwidth, I_d is the dark current, K_B =1.3807 x 10⁻²³ joules per kelvin (J·K⁻¹) is the Boltzmann's constant, T is the absolute temperature, R_L is the equivalent load resistance, P_B is the background noise power and R_0 in mA/watt is the detector responsivity given by

$$R_0 = \frac{\eta q}{h \nu}$$

where η is the detector quantum efficiency, $q = 1.602 \times 10^{-19}$ Coulomb is the electronic charge, $h = 6.623 \times 10^{-34}$ Joule.sec is the Planck's constant, ν the operating frequency.

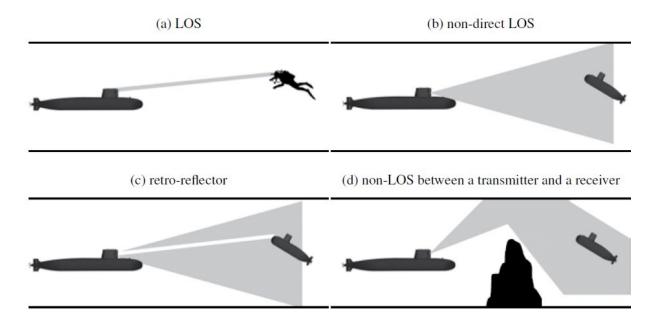
When APD is used, the dark current and shot noise are increased by the multiplication process; however, the thermal noise remains unaffected. Therefore, if the photocurrent is increased by a factor of M avalanche multiplication factor, then the total shot noise is also increased by the same factor. For the surface dark current I_{ds} =0, the direct detection SNR for APD photodetector is

$$SNR = \frac{\left(MR_{0}P_{R}\right)^{2}}{2qB\left(R_{0}P_{R} + R_{0}P_{B} + I_{db}\right)M^{2}F + 4K_{B}TB/R_{L}}$$

where F is the excess noise factor arising due to random nature of multiplication factor, I_{db} is the bulk dark current.

Since the photodetector response is insensitive to the frequency, phase, or polarization of the carrier, this type of receiver is useful only for intensity-modulated signals.

13. Optical Wireless Communication in Underwater Medium



Different underwater optical wireless link configuration.

Optical wireless communications are a relatively new technology providing many serious advantages, such as the very high rates of data transmission, secure links, very small and light.

Optical waves in the visible spectrum (400–700 nm) present an alternative way to provide broadband communications in the water. They propagate faster in water (300,000,000 m/s) than the acoustic ones (340 m/s in air, 1500 m/s in water), which is about 200,000 times faster than sound travels through water. That is the main reason why they have gained a considerable interest during the last years to serve as a broadband (10–100 Mbps), safe (non-interceptable) and reliable complement to acoustic underwater communications systems.

In general, optical signals are highly absorbed in water, and this is one of the main disadvantages; the other one is the optical scattering by all the particles existing inside the sea. However, seawater shows a decreased absorption in the blue/green region of the visible spectrum. Thus, using suitable wavelengths, for instance in the blue/green region, high speed connections can be attained according to the type of water (400-500 nm) for clear to 300-700 nm for turbid water conditions). Minimum attenuation is centered near $0.460 \text{ }\mu\text{m}$ in clear waters and shifts to higher values for dirty waters approaching $0.540 \text{ }\mu\text{m}$ for coastal waters.

The power received P(z), given initial power P_0 , propagating through a medium of thickness z is estimated by the Beer's Law given by

$$P(z) = P_0 e^{-c(\lambda)z}$$

where $c(\lambda)$ in m^{-1} is the extinction coefficient expressing the total attenuation occurred by the propagation through the water.

The total attenuation can be described as the sum of absorption and scattering. Thus,

$$c(\lambda) = \alpha(\lambda) + \beta(\lambda)$$

where $\alpha(\lambda)$ is the absorption coefficient, $\beta(\lambda)$ is the scattering coefficient and the product cz is the attenuation length, and it contributes on the reduction of the received power by a factor of exp(-1), or $\sim 63\%$.

Beer's Law provides a limited applicability as it describes only the attenuation due to absorption and single scattering events. In reality, however, many cases of multiple scattering may occur. Also it presumes that the source and receiver are in exact alignment with each other, and it can be applied only in Line-of-Sight (LOS) communication scenarios. Moreover, Beer's Law ignores temporal dispersion.

More accurate expressions have to take the link geometry into account. For instance, assuming that the transmitter and receiver are positioned in a non LOS configuration, the received power dependent on time t, lateral displacement from the beam axis r, and range z is

$$P_{R}(t,r,z) = P_{T}(t)D_{T}L_{w}(t,r,z)D_{R}$$

where $P_T(t)$ is the transmitted power, D_T is the aperture and divergence of the optical source, and D_R is the photoreceiver aperture and field of view. The channel loss term, $L_w(t,r,z)$, characterizes the spatial and temporal characteristics of light propagation in seawater.

UOWC propagation

Underwater medium characteristics

Underwater medium contains almost 80 different elements, dissolved or suspended in pure water, with different concentrations. Some of them are

- Various dissolved salts such as NaCl, MgCl2, etc, which absorb light at specific wavelengths and induce scattering effects.
- Minerals like sand, metal oxides, which contribute to both absorption and scattering.
- Colored dissolved organic matters such as fulvic and humic acids which affect absorption, mainly in blue and ultraviolet wavelengths.
- Organic matters such as viruses, bacteria, and organic detritus which add backscattering, especially in the blue spectral range.
- Phytoplankton with chlorophyll-A which strongly absorbs in the blue-red region and scatters green light.

Since chlorophyll absorbs the blue and red wavelengths and the particles strongly contribute to the scattering coefficient, we can use its concentration C (in mg/m³) as the free parameter to calculate the absorption and scattering coefficients.

The exact type of water plays a significant role in the estimation of the amount of chlorophyll concentration and consequently the amount of absorption and scattering for a specific geographic location. A classification system for the clarity of water types based on their spectral optical attenuation depth was proposed by Jerlov.

The four major water types are

- Pure deep ocean waters cobalt blue where the absorption is high and the scattering coefficient is low.
- Clear sea waters with higher scattering due to many dissolved particles.
- Near coasts ocean waters with absorption and scattering due to planktonic matters, detritus and mineral components.
- Harbor murky waters, which are quite constraining for optical propagation due to dissolved and insuspension matters.

Absorption

The absorption coefficient, $\alpha(\lambda)$ is the ratio of the absorbed energy from an incident power per unit distance due to various dissolved particles such as phytoplankton, detritus, etc.

$$\alpha(\lambda) = \alpha_w(\lambda) + \alpha_c^0(\lambda) (C_c/C_c^0)^{0.602} + \alpha_f^0 C_f e^{-k_f \lambda} + \alpha_h^0 C_h e^{-k_h \lambda}$$

where $\alpha_w(\lambda)$ is the absorption by the pure water in m⁻¹, λ is the wavelength in nm, $\alpha_c^0(\lambda)$ is the absorption coefficient of chlorophyll in m⁻¹, C_c is the total concentration of chlorophyll per cubic meter $(C_c^0 = 1 \text{mg/m}^3)$, $\alpha_f^0 = 35.959 \text{ m}^2/\text{mg}$ is the absorption coefficient of fulvic acid, $k_f = 0.0189 \text{ nm}^{-1}$, $C_f = 0.0189 \text{ mg}^{-1}$

0.0189 nm⁻¹, $\alpha_h^0 = 18.828 \text{ m}^2/\text{mg}$ is the absorption coefficient of humic acid and $k_h = 0.01105 \text{ nm}^{-1}$. The concentrations C_f and C_h are expressed as

$$C_f = 1.74098 C_c e^{0.12327 \left(C_c/C_c^0\right)}$$

$$C_h = 0.19334 C_c e^{0.12343 \left(C_c/C_c^0\right)}$$

Scattering

Scattering coefficient, $\beta(\lambda)$ is the ratio of energy scattered from an incident power per unit distance. It is the sum of backward scattering, $\beta_b(\lambda)$ and forward scattering coefficient, $\beta_f(\lambda)$.

Scattering is caused by small and large particles. Small particles are the particles with refractive index equal to 1.15, whereas large particles have a refractive index of 1.03. The scattering and backscattering coefficients are

$$\beta(\lambda) = \beta_w(\lambda) + \beta_s^0(\lambda)C_s + \beta_l^0(\lambda)C_l$$

$$\beta_{R}(\lambda) = 0.5 \beta_{w}(\lambda) + 0.039 \beta_{s}^{0}(\lambda) C_{s} + 6.4 \times 10^{-4} \beta_{l}^{0}(\lambda) C_{l}$$

For small and large particulate matter

$$\beta_s^0(\lambda) = 1.151302 \left(\frac{400}{\lambda}\right)^{1.7}$$

$$\beta_l^0(\lambda) = 0.341074 \left(\frac{400}{\lambda}\right)^{0.3}$$

and the concentrations are

$$C_s = 0.01739 C_c e^{0.1163 \operatorname{l}\left(C_c/C_c^0\right)}$$

$$C_I = 0.76284 C_c e^{0.03092 \left(C_c/C_c^0\right)}$$

Oceanic turbulence

Optical wireless communications are greatly affected by optical turbulence, which refers to random fluctuations of the refraction index.

In the case of underwater systems, these fluctuations are mainly caused by variations in temperature and salinity of the oceanic water.

An important parameter for the description of oceanic turbulence is the scintillation index, which expresses the variance of the wave intensity.

Link budget

Empirical path loss models are effective enough to estimate the received optical power for underwater communications under LOS conditions.

$$P_{R} = P_{T} \eta_{t} \eta_{r} e^{-\frac{c(\lambda)R}{\cos \theta}} \frac{A_{R} \cos \theta}{2\pi R^{2} (1 - \cos \theta_{0})}$$

where P_T is the transmitted power, η_t and η_r are the optical efficiencies of the Tx and Rx correspondingly, $c(\lambda)$ is the extinction coefficient, R is the perpendicular distance between the Tx plane and the Rx plane, θ_0 is the Tx beam divergence angle, θ is the angle between the perpendicular to the Rx plane and the Tx-Rx trajectory, and A_R is the receiver aperture area.

14. All Optical Networking

All optical networks aim at very high data rates in the overall telecommunication network by replacing all the network elements by optical elements.

- High-capacity telecommunications networks.
- Based on all optical components.
- All the network is to be designed with all optical elements, thus bandwidth will not be a limiting factor since opto electronic conversions will not be needed throughout the network.

General considerations in all optical networks:

Electro/Optics and Opto/electronic conversions limit the use of optical network advantage in very high data bit rates because electronics can not handle very high data rates as the optics can handle.

Without optical Add-Drop Multiplexers, each location that demultiplexes signals will need an electrical network element for each channel, even if no traffic is dropping at that site.

By implementing an optical network, only those wavelengths that add or drop traffic at a site need corresponding electrical nodes. Other channels can simply pass through optically, which provides tremendous cost savings in equipment and network management.

In addition, performing space and wavelength routing of traffic avoids the high cost of electronic cross-connects.

Wavelength Services: In optical networks, service providers are able to resell bandwidth rather than fiber. By maximizing capacity available on a fiber, service providers can improve revenue by selling wavelengths, regardless of the data rate required. To customers, this service provides the same bandwidth as a dedicated fiber.

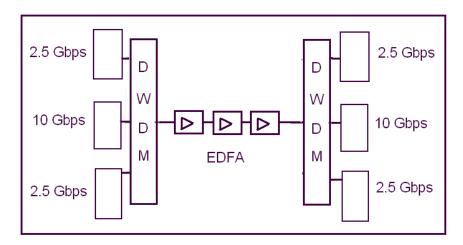
Currently employed optical elements in the telecommunications network:

• Optical fibers:

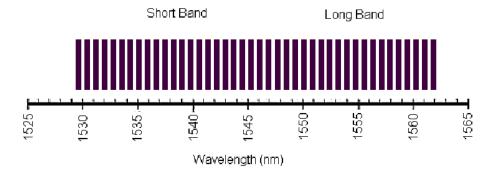
First, more capacity between two sites meant the installation of more fibers.

Then more time division multiplexed (TDM) signals are placed in the same fiber, i.e. the bandwith handling capability of the fibers were increased. (both through fiber manufacturing and semiconductor laser modulation techniques supporting high rates of 40 Gbps.)

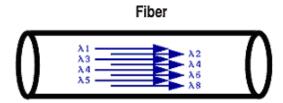
Optical networks with Dense Wavelength Division Multiplexing (DWDM) provide additional capacity
on existing fibers. DWDM is introduced providing many virtual fibers on a single physical fiber which
increased drastically the information rate carrying capability of fibers (in the order of hundreds of
Terabits per second).



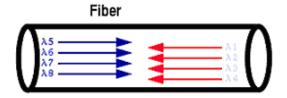
- ITU Channel Spacing is shown below:



- Two basic types of DWDM:
 - i. Unidirectional: All the wavelengths travel in the same direction on the fiber



ii. Bidirectional: Signals are split into separate bands, with both bands traveling in different directions.



- SDH/SONET.
- Optical Amplifiers
 - Erbium-Doped Fiber Amplifier (EDFA). By doping a small strand of fiber with a rare earth metal, such as erbium, optical signals could be amplified without converting the signal back to an electrical state.
 - EDFA operating at 1550 nm is used at each 50 100 km and replaces electronic regenerators.
 - EDFA enables data rates of 10 Gbps or higher. With the electronic conversion the rate was limited by 2.5 Gbps.
- Laser diodes used in optical fiber communications.
- LED light sources.
- Optical detectors used in optical fiber communications.
- Tunable Lasers:

Radiate light at different wavelengths.

Can switch from one wavelength to another very quickly.

Narrowband Lasers

Advanced lasers have extremely narrow source spectral bandwidths (<< 1 nm), very narrow wavelength spacings.

Long-haul applications use externally modulated lasers, while shorter applications can use integrated laser technologies.

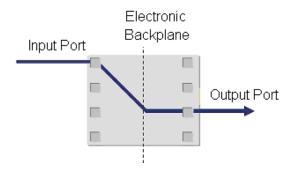
Optical elements that are not yet currently employed in the telecommunications network:

• Optical Switches (Sometimes referred to as Optical Cross Connects or Wavelength Routers)

Switch takes traffic in electrical form from an input port or connection and directs it again in electrical form over a backplane, to an output port.

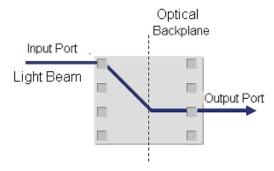
Electronic switches direct variable-length packets, fixed-length cells, and synchronous timeslots from an input port to an output port.

An electronic space switching is shown below:



An optical switch works with light. It directs a light beam of a single wavelength or of a range of wavelengths from an input port to an output port.

An optical space switching is shown below:



A switch needs some kind of information to make the switching decision. In electronic switches, this information is carried inside packets.

An IP switch, or router, uses the destination IP address (IP_D) to make its decision.

The criterion of the optical switch for making a forwarding decision is carried in the so called digital wrapper around each input wavelength of the light.

Wrapper is equivalent to packet header which carries information such as what type of traffic is in the wavelength, where the traffic is headed, ... etc.

As the wavelength moves around the network, the nodes read the wrapper and get the information for originating and terminating details, whether it carries an IP or ATM or another protocol signal, commands such as error correction and whether the wavelength needs to be rerouted.

Types of Optical Switches:

• <u>MEMS</u> (Micro Electro Mechanical System) Switches:

Light in one fiber is just redirected to move to a different fiber by using microscopic (with diameters of a human hair) moveable (moveable in three dimensions) mirrors (several hundred mirrors placed together on mirror arrays in an area of a few centimeters square).

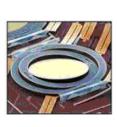
Light from an input fiber is aimed at a mirror, which is directed to move the light to another mirror on a facing array.

Light beams themselves tell the mirror (through digital wrappers) what bend to make in order to route the light appropriately.

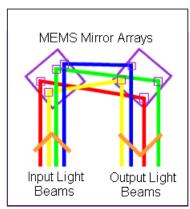
This mirror then reflects the light down towards the desired output optical fiber.

There exists designs of $1,024 \times 1,024$ wavelengths (if each can carry 40 Gbps it corresponds to a capacity of 40 Gbps x 1,024 = 40.96 Tbps) in an area of around 25 cm x 15 cm.

Picture of a MEMS mirror and MEMS mirror array deflection mechanism are shown below:







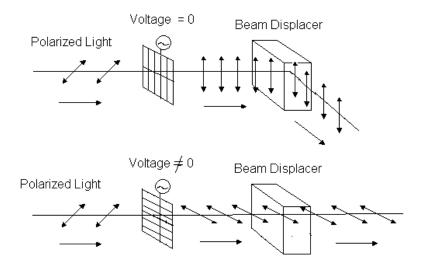
- Buble Switches: Use heat to create small bubles in fluid channels which then reflect and direct light
- Thermo-optical Switches:

Light passing through glass is heated up or cooled down by using electrical coils.

Heat alters the refractive index of the glass, bending the light to enter one fiber or another.

• Liquid Crystal (LCD) Switches:

Use liquid to bend light



Liquid Crystal Cell

Wavelength Switching:

Single wavelength enters the switch

A "wavelength" selection is made by using prisms, filters or gratings.

Based on the wavelength selected, the light is switched to a known output port.

• Optical Burst Switching:

Disadvantage of lambda switching is that, once a wavelength has been assigned, it is used exclusively by its "owner."

If 100 percent of its capacity is not in use for 100 percent of the time, then there is an inefficiency in the network.

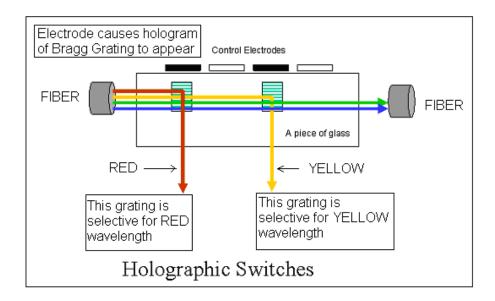
A solution to this is to allocate the wavelength for the duration of the data burst being sent giving rise to optical burst switching.

• Optical Packet Switching (OPS):

OPS is the optical equivalent of an electronic packet switch, reading the embedded label and making a switching decision using this information.

• Holographic Switching:

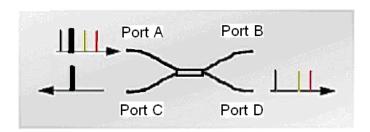
- Creates a wavelength-specific reflective grating, but does this dynamically.
- The grating structure in these devices is written as a hologram into a piece of glass.
- The holograms are "invisible" until they are energized by a set of control electrodes.



• Optical Add/Drop Multiplexers

Fiber Bragg Gratings

- It is a small section of fiber modified to create periodic changes in the index of refraction.
- Depending on the space between the changes, a certain frequency of light the Bragg resonance wavelength is reflected back, while all other wavelengths pass through.



- Optical filters: Fiber Bragg gratings are also used in signal filtering.
- Multiplexers, demultiplexers

Thin Film Substrates

- By coating a thin glass or polymer substrate with a thin interference film of dielectric material, the substrate can be made to pass through only a specific wavelength and reflect all others.
- By integrating several of these components, optical network devices such as multiplexers, demultiplexers and add/drop devices are designed.